

Machine Learning in Finance Workshop 2020

AGENCY MBS PREPAYMENT MODEL USING NEURAL NETWORKS

Jiawei “David” Zhang

MSCI

 COLUMBIA UNIVERSITY
Data Science Institute



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The Fu Foundation School of Engineering and Applied Science

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AGENCY MBS PREPAYMENT MODEL USING NEURAL NETWORKS

Columbia Bloomberg Machine Learning in Finance 2020

David Zhang

MSCI Securitized Products Research



Speaker



David Zhang, PhD

New York

**MANAGING DIRECTOR, HEAD OF
SECURITIZED PRODUCTS RESEARCH**

T 212.981.7464

E david.zhang@msci.com

David Zhang is a Managing Director and Head of Securitized Products Research at MSCI. His team is responsible for developing models and analytics to support investment analysis, risk management, and regulatory compliance. Before joining MSCI, Dr Zhang was Managing Director and head of Securitized Products modeling at Credit Suisse for more than a decade. At Credit Suisse he was responsible for supporting risk, regulatory and client analytics as well as sales/trading quantitative strategies. Dr Zhang's group developed one of the most widely used MBS models by fixed income institutional investors. Their work was consistently awarded top ranking by various industry and client surveys, including Institutional Investor All-America Research Team ranking in Agency prepayment. They also won the award for best paper by the American Real Estate Society for research on effectiveness of government mortgage programs. The regulatory projects Dr Zhang lead at Credit Suisse included developing models for CCAR and PPNR (Pre-Provision Net revenue), Dodd-Frank IHC (Intermediate Holding Company) and related VaR, RWA and RBPL modeling, and FRTB (Fundamental Review of Trading Book). Prior to Credit Suisse, Dr Zhang worked at FreddieMac, CIBC Oppenheimer, and University of Chicago. He holds leadership positions at PRMIA (Professional Risk Management International Association) and GCREC (Global Chinese Real Estate Congress). He is a frequent speaker at industry and academic conferences, and his research on risk, financial modeling and real estate has been published in many academic journals. Dr Zhang has a Ph.D. from Princeton University.

SUMMARY: NEURAL NETWORKS AGENCY MBS PREPAYMENT MODEL

Why a machine learning model for Agency MBS?

- Prepayment is a highly complex and non-linear process with many idiosyncratic risk factors, among the most complex financial models
- Recent development in computational software and hardware enable us to make significant advancement in AI prepayment models
- Machine learning models have excelled in many areas, such as image recognition, natural language processing, fraud detection, etc.

What is the model and what have we learned?

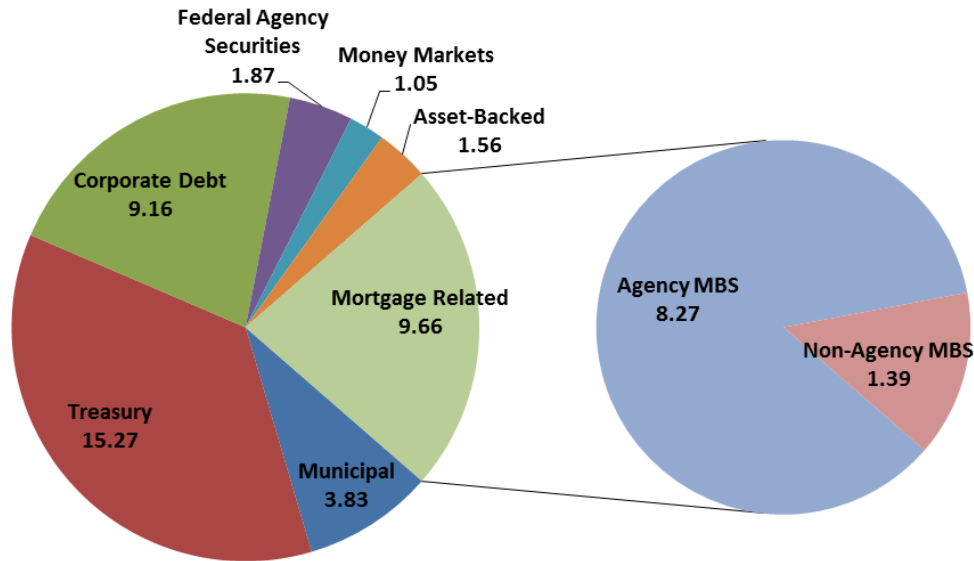
- Deep neural network model applied to pool level agency MBS prepayment data, compared with MSCI1 (the human model)
- Results show the deep learning model is able to capture very complex prepayment patterns and signals with extremely high computational efficiency

MACHINE LEARNING IN FINANCE

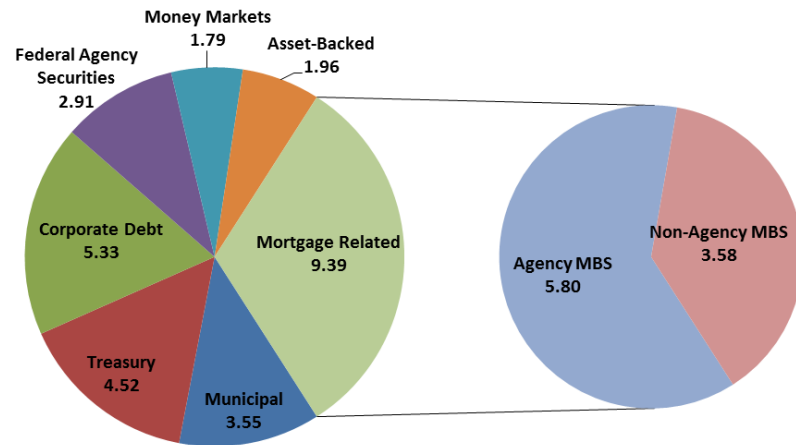
- **Consumer credit risk models via Machine-Learning Algorithms (Dr. Andrew Lo, 2010)**
 - Using machine-learning model for consumer credit default and delinquency
 - Generalized classification and regression trees
 - Accurately forecasted credit events 3 to 12 months in advance
- **Risk and risk management in credit card industry (Dr. Andrew Lo, 2016)**
 - Analyzed very large dataset consisting of credit card data from six large banks.
 - Decision trees and random forests model perform better than logistic regression at short time horizon
- **Deep learning for mortgage risk (Dr. Kay Giesecke, 2015-2018)**
 - Using deep neural network to model mortgage prepayment, delinquency and foreclosure
 - Loan level data
 - Compared NNM with a logit model

US BOND MARKET

US Bond Market 2018 (42.4\$Tn)



US Bond Market 2007 (29.5\$Tn)



MODELING OBJECTIVE

Forecast prepayment rate for agency RMBS pools

SMM : Single Monthly Mortality Rate

CPR: Conditional Prepayment Rate

Agencies report last month's prepayment speed on the 4th business day of each month.

Prepayment types:

- Rate refinance
- House turnover
- Cash-out
- Curtailment
- Buyout

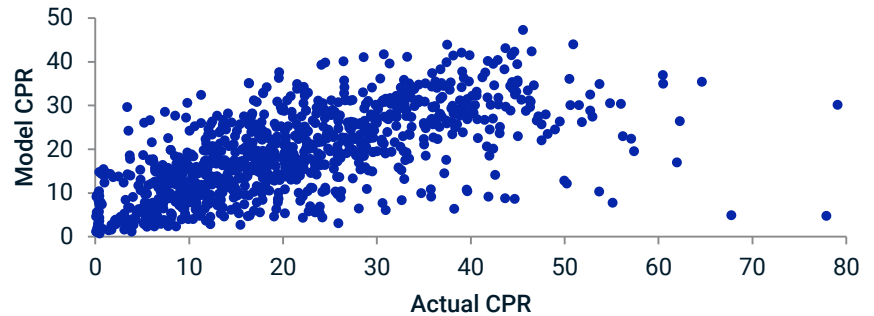
MORTGAGE PREPAYMENT MODELING: SCIENCE AND CRAFTSMANSHIP

Difficulties with mortgage prepayment modeling

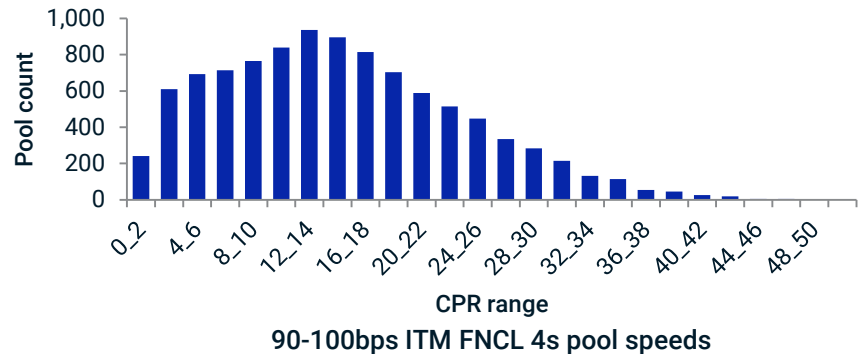
- Large data sets: ~20-2000 G data, Agency MBS covers ~400,000 pools/100+mm loans performance over 20-30 years, pool/loan variables ~30-100
- Multiple, highly non-linear and interactive risk drivers (“layered risk”)
 - Loan size vs. prepayment is function of moneyiness
 - Age vs. prepayment is function of past moneyiness history
 - Loan purpose (refi vs purchase) vs. prepayment is function of origination year
 -
- Regime changes
 - Mortgage credit and borrower risk appetite cycles, and business practice affect absolute level and risk drivers for prepayment/default

► Agency MBS prepayment

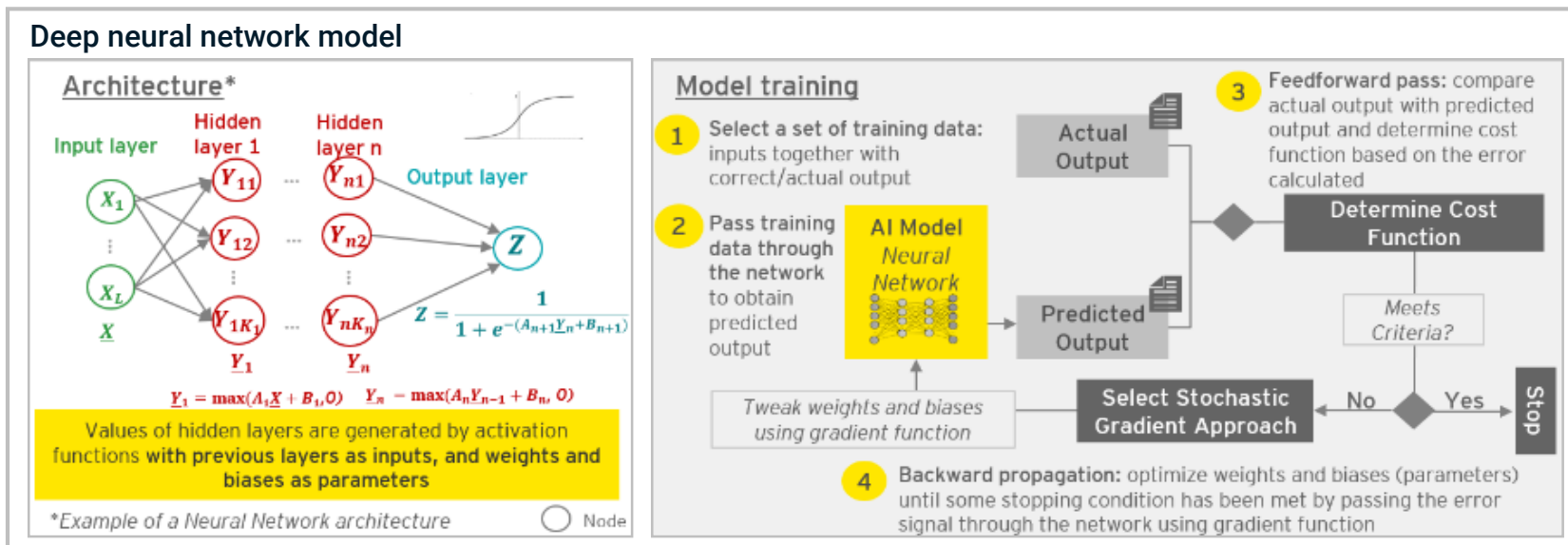
- Complex behaviors
 - 30–100 risk factors: rates, loan size, GEO, purpose, property, HPA....
 - “layered risk”- non-linear interaction (e.g., loan size vs moneyiness, purpose vs. origination year, ..)
 - Regime changes: behavior, policy
 - Statistical noises
- Large data set to model
 - 400,000 pools/100m loans, 30yr
- Modelers as craftsman?
 - Idiosyncratic modeler risk



Model CPR distribution



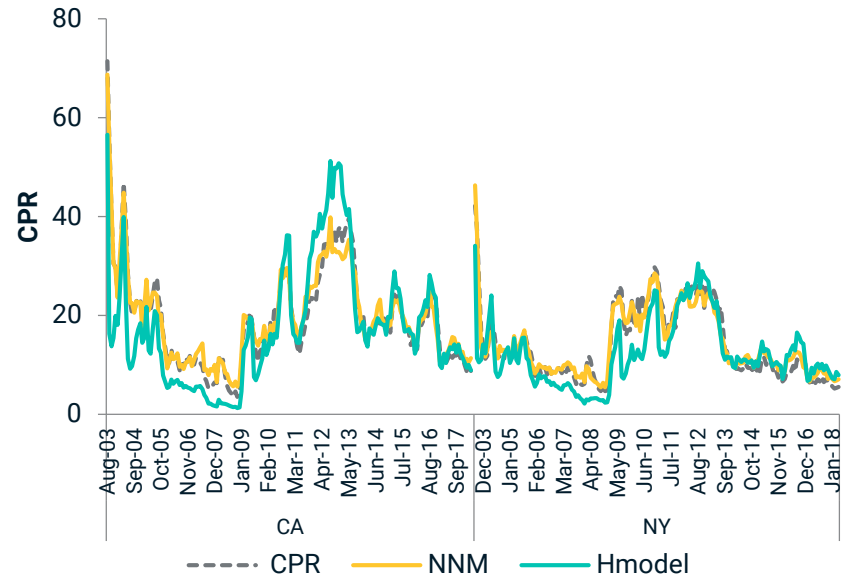
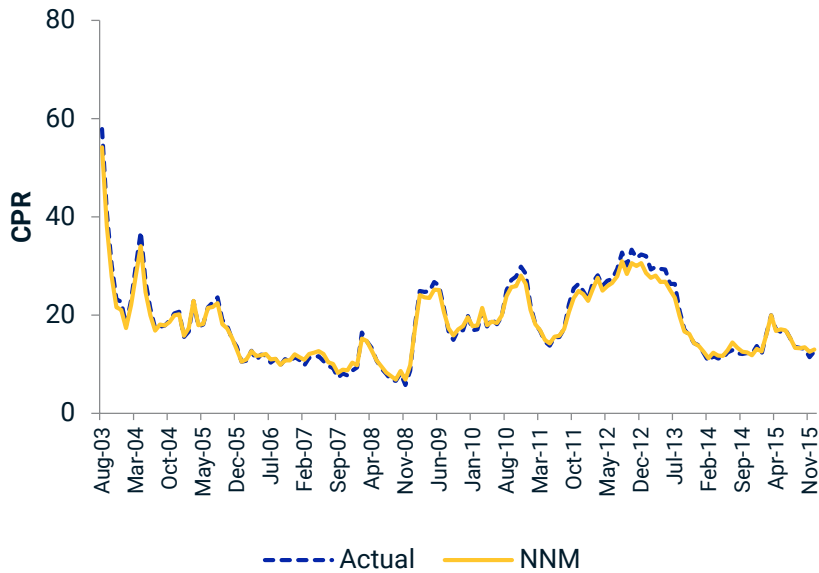
▶ AI agency MBS prepayment model



- Feed forward neural network
 - Applied successfully in many other fields
 - Layers and nodes, hyper-parameters
 - Ensemble techniques, bagging and boosting

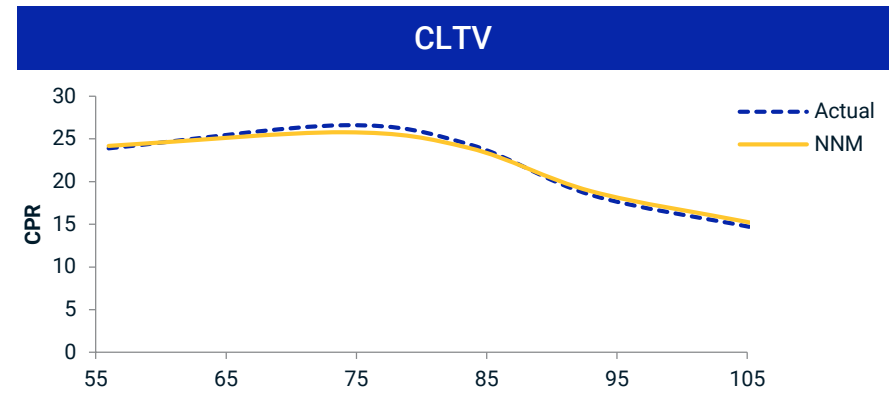
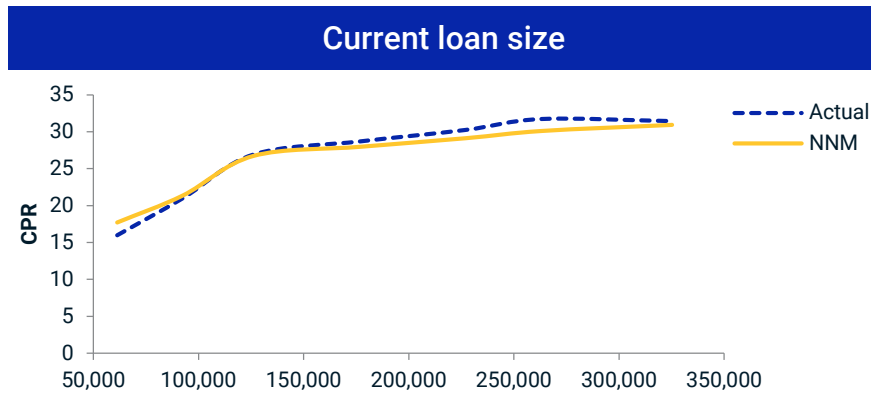
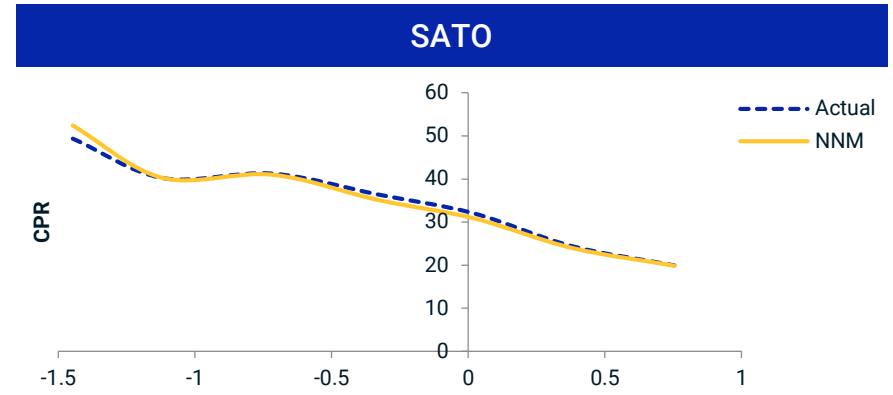
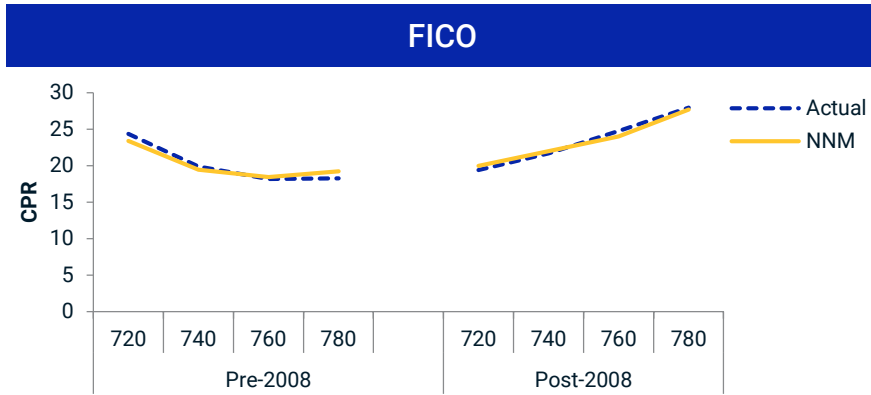
- Competing vs. “human” /MSCI production model
 - Forecast accuracy
 - New signals, new discoveries
 - x100-1000 Efficiency gains: 3hrs vs. weeks/months

▶ AI vs. “human” models: higher accuracy



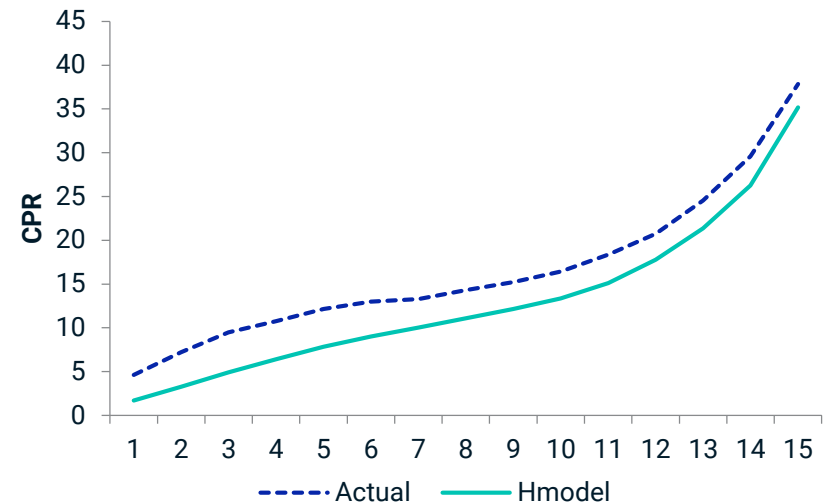
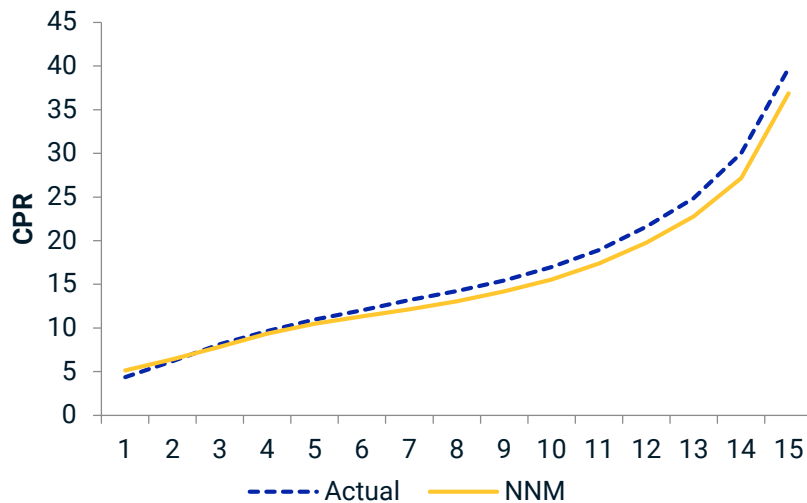
- Higher modeling accuracy
 - Across cohorts and multiple dimensions of risk factors
 - Highly adaptive to high dimensionality and non-linearity

▶ AI vs. “human” models: higher accuracy



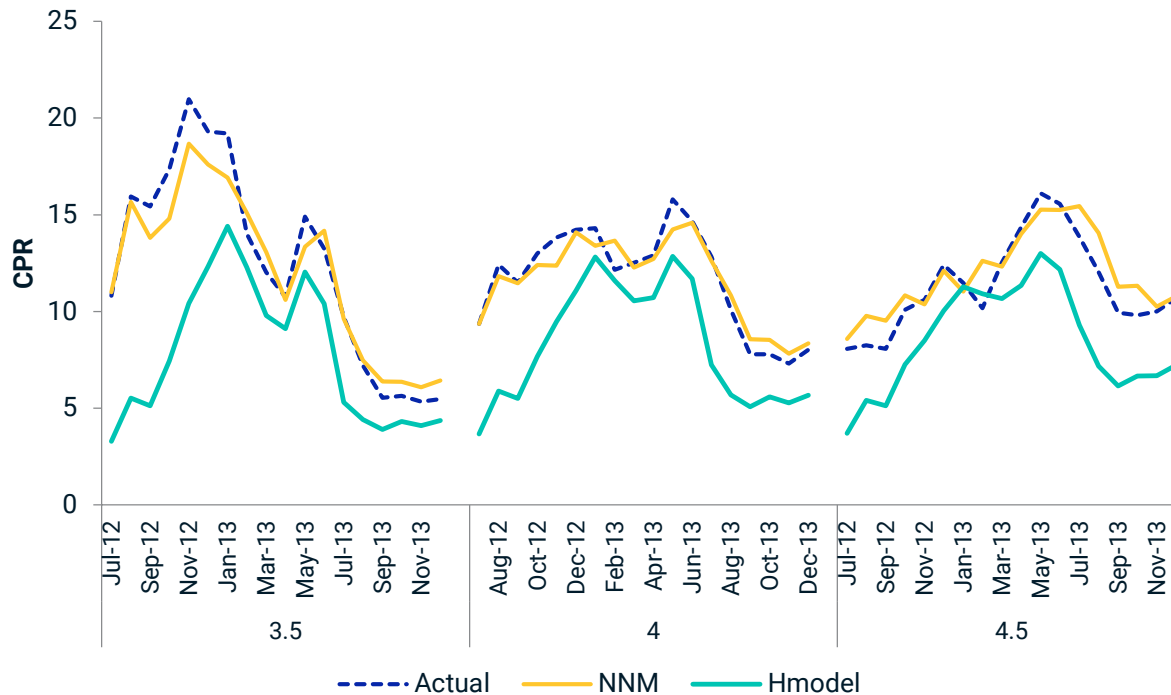
▶ AI vs. “human” models: higher accuracy

Ranking based sample error tracking for FNCL 4s



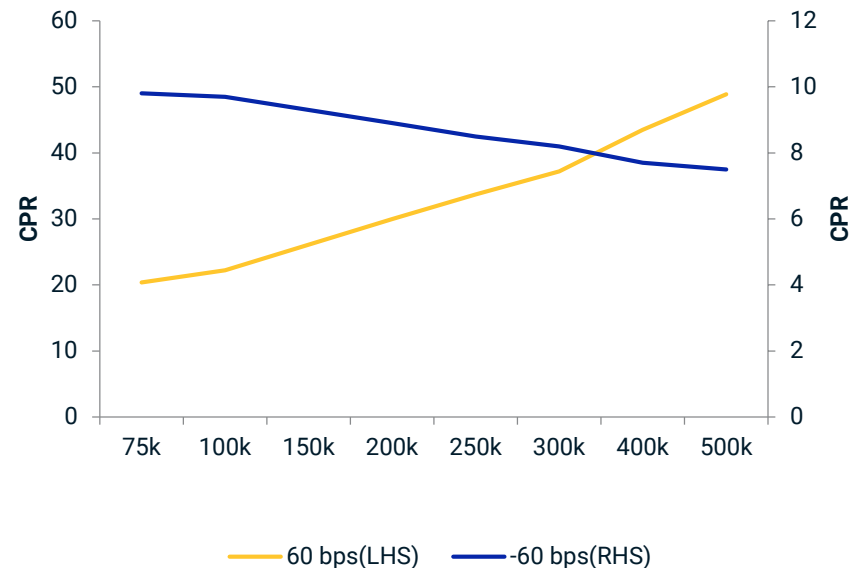
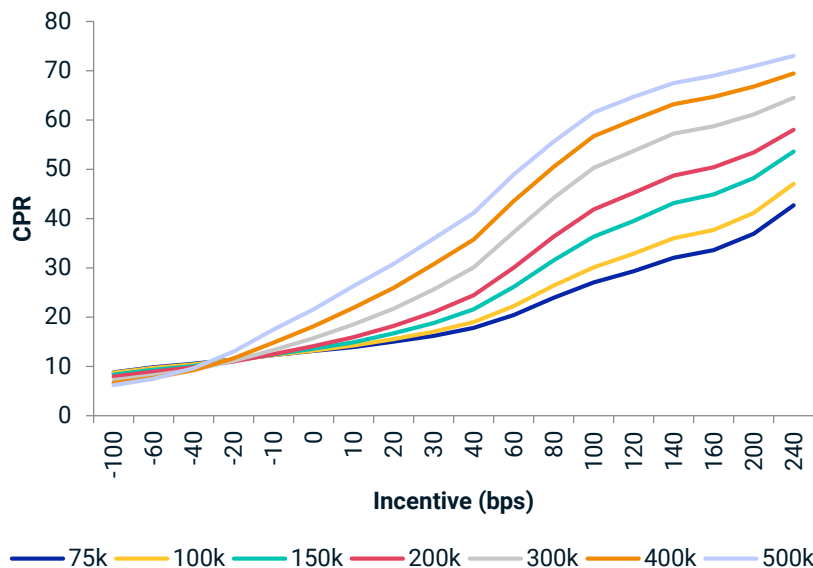
- Higher modeling accuracy
 - Across cohorts and multiple dimensions of risk factors
 - Highly adaptive to high dimensionality and non-linearity

▶ AI vs. “human” models: higher accuracy



- “Media effect”
 - When rates hit historical low, new & lower coupons ramp up faster
 - Highly non-linear behavior and depends on multiple risk factors

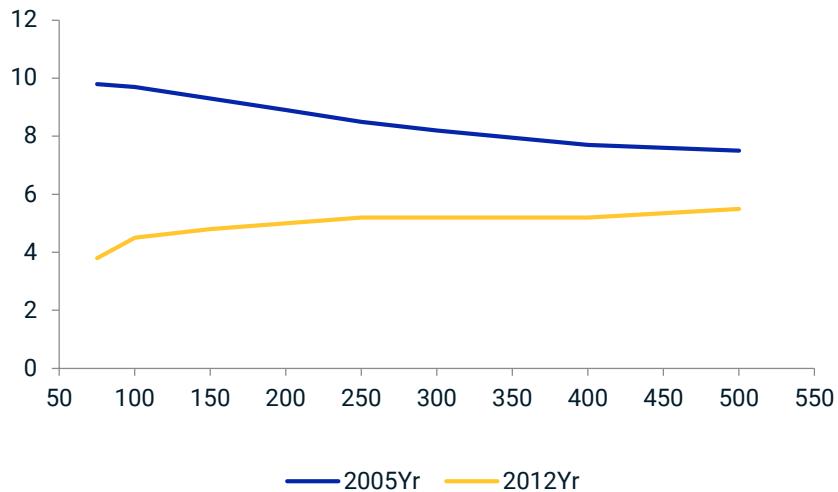
▶ AI vs. “human” models: new signals



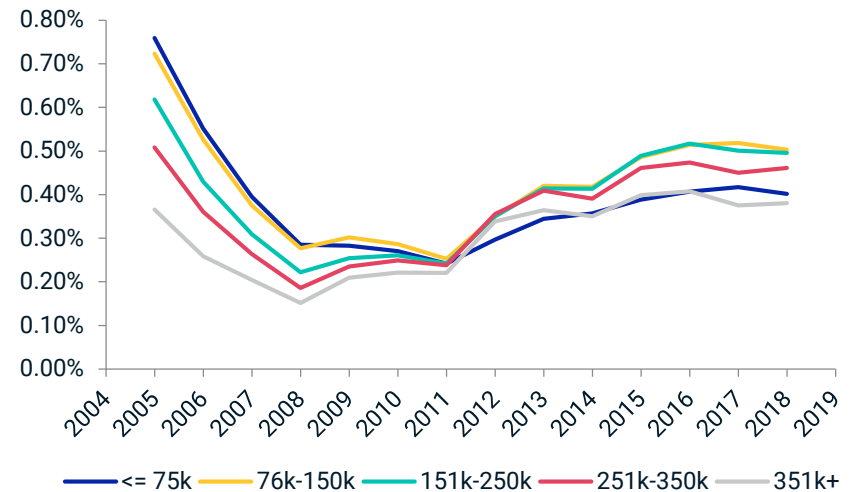
- Accuracy vs overfitting: loan size example
 - Understand sensitivities of risk drivers and economic rationale
 - Apply regularization to penalize overfitting

▶ AI vs. “human” models: new signals

Model speeds for OTM 60bps vs loan size (in thousands)



Housing turnover vs loan size and year*



- Is low loan balance still safe investment for extension risk?
 - Sensitivity tests for the AI model indicate relationship between loan size and housing turnover has flipped after the recession
 - This is verified by Black Knight’s proprietary data

CONCLUSION

NN model vs. “Human Model”

- Accurate forecasts and successfully flag prepayment anomalies **over the study period**
- Accurate model large numbers of risk factors
- Accurate model highly non-linear and interactive risk factors
- Highly efficient modeling process - hundreds times of increases in modeling efficiency
- **Was** able to find/flag prepayment signals that eluded human models

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Siyu Lin:

Senior Quantitative Analysts, Quantitative Advisory Services , Ernst & Young

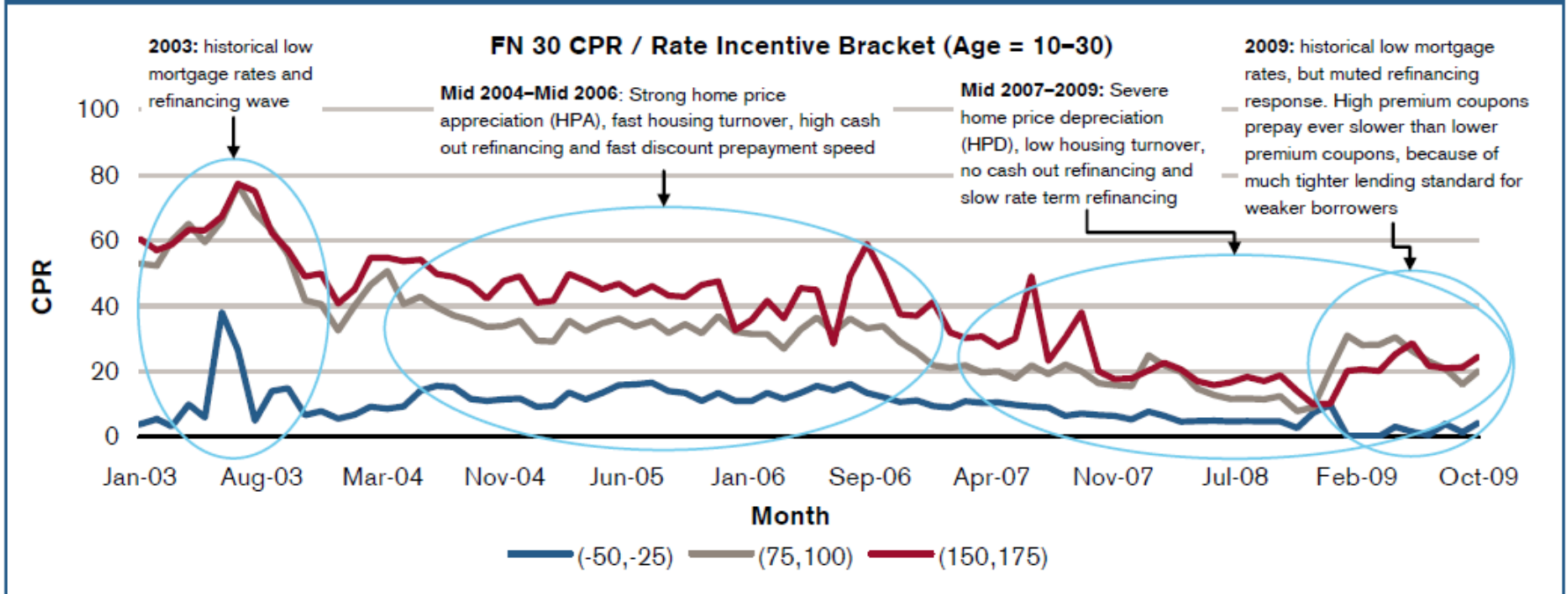
Henry Li:

Executive Director, in Quantitative Advisory Services practice, Ernst & Young

Appendix

MORTGAGE PREPAYMENT MODELING: SCIENCE AND CRAFTSMANSHIP

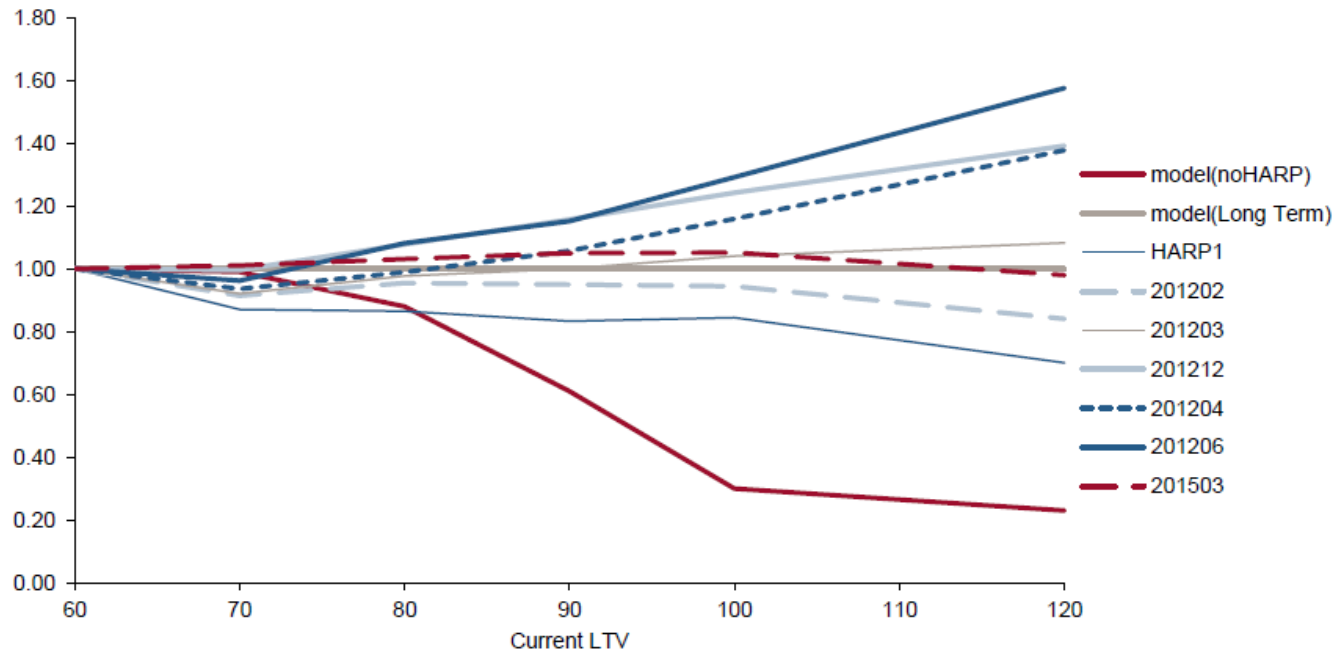
Exhibit 4: Agency MBS prepayment regimes since 2003



MORTGAGE PREPAYMENT MODELING: SCIENCE AND CRAFTSMANSHIP

Exhibit 5: HARP CLTV curve history and long term model assumptions

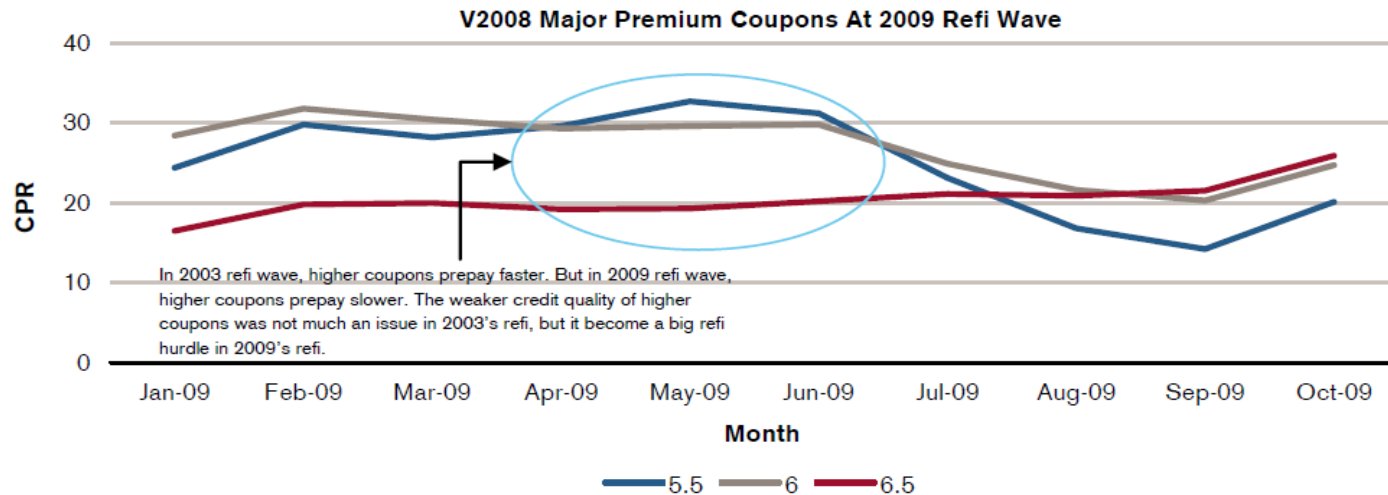
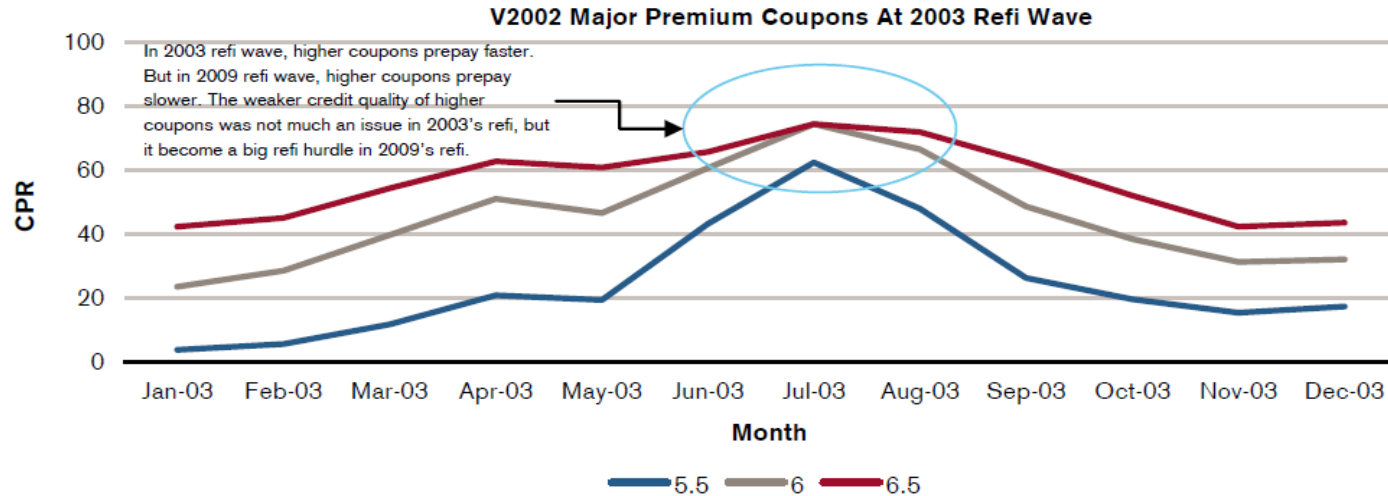
The CLTV curve represents the ratio of refinance speeds across CLTV spectrum, using sub-50 CLTV cohort as benchmark, with all other pool variables (for example, loan size, moneyness, FICO, etc.) holding constant



The HARP program caused temporary inversion of the CLTV Prepayment Curve

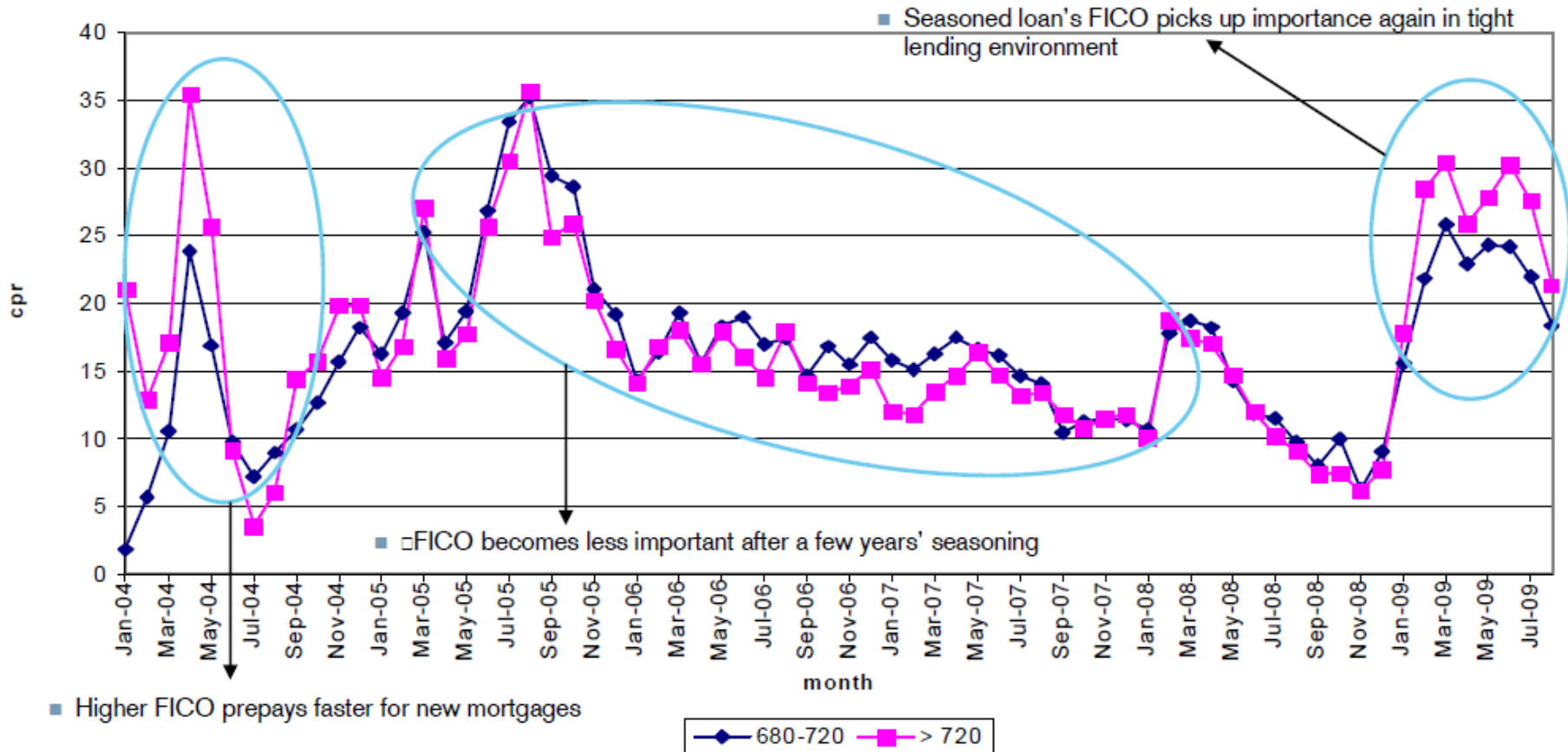
HARP: Home Affordable Refinance Program

MORTGAGE PREPAYMENT MODELING: SCIENCE AND CRAFTSMANSHIP



MORTGAGE PREPAYMENT MODELING: SCIENCE AND CRAFTSMANSHIP

FN30 6.0 V2004 CPR / Fico (owner occ, clsz=100K-150K,oltv < 80)



MORTGAGE PREPAYMENT MODELING: SCIENCE AND CRAFTSMANSHIP

Example of modeling:

Assume ppm (pool, time) = $f(X_1, X_2, X_3, \dots, X_n)$...

start by assuming separable risk factor: $\text{ppm} = f_1(x_1) * f_2(x_2) \dots$ Until (often) proven incorrect...

estimating $f_1(x_1)$ by “building cohort”, by bucketing loans/pools for groups of x_1 , but similar $x_2, x_3 \dots$

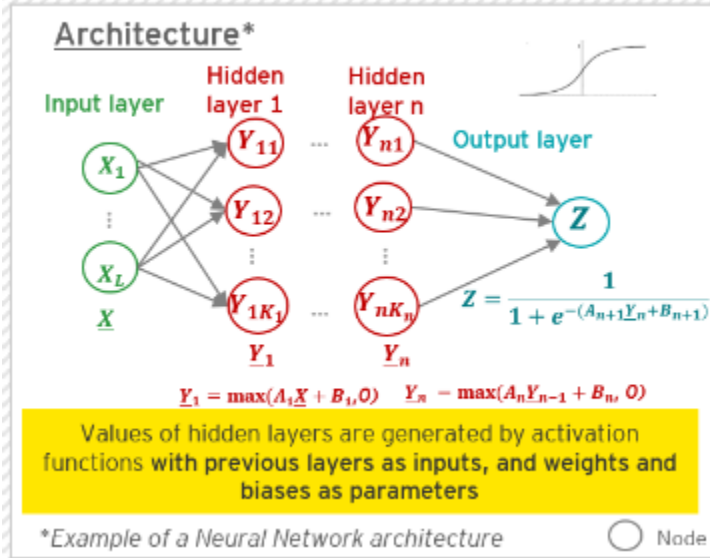
(this further assumes quasi linear property of $x_2, x_3 \dots$ $\text{Average}(f_2(x_2) f_3(x_3) \dots) = f_2(\text{ave}(x_2)) * f_3(\text{ave}(x_3)) \dots$

..... Checking overall fit after all X_n are fitted, adding extra variables to deal with non-linear and interactive variables... this often does not lead to convergence ...

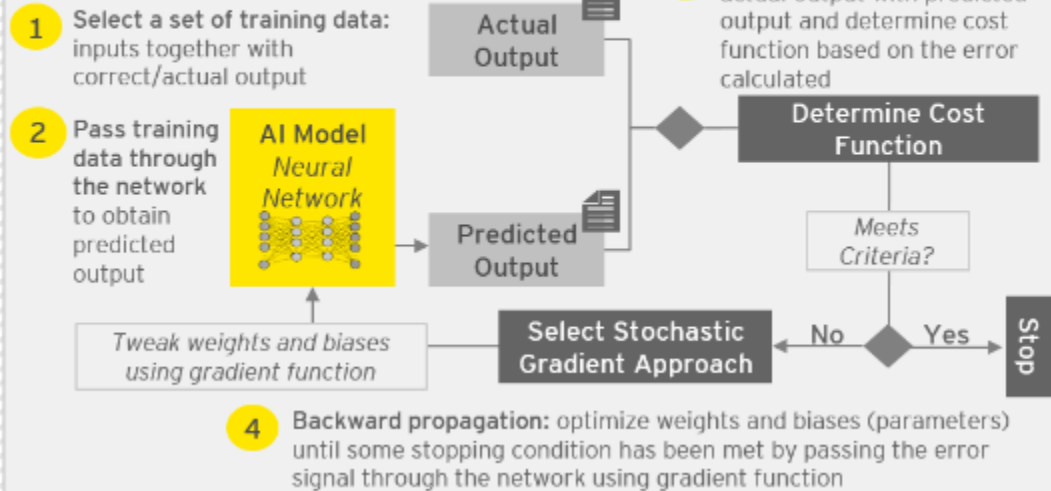
- Time consuming and non-standard approaches
- Experience and step-by-step / regime-by-regime progress are valued
- Can new techniques of AI modeling provide the much needed disruption?

FEED FORWARD NEURAL NETWORK

Deep neural network model



Model training



Network architecture:

Layers and nodes

Hyper-parameters

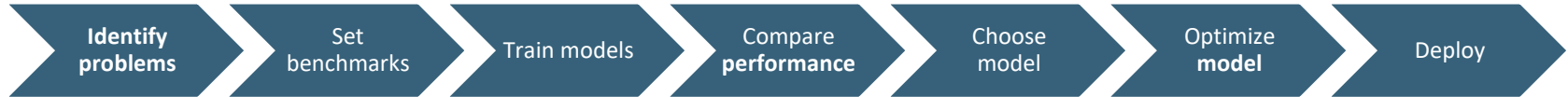
Batch size, number of nodes, learning rate, max-norm constraint, dropout rate

Ensemble techniques:

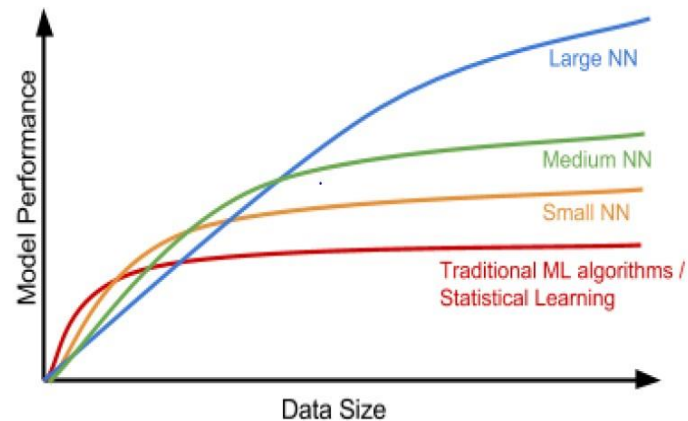
Bagging: minimum MSE of different realizations and neural networks

Boosting: Fine tune a neural network via changing a few hyper-parameters

TRADITIONAL VS.. DEEP MACHINE LEARNING



Traditional learning algorithm		Deep Learning	
Pros	Cons	Pros	Cons
Works better on smaller data	Hard to scale	state-of-the-art for certain domains, such as computer vision and speech recognition.	require large amount of data.
Financially and computationally cheap	Lack of variability	Perform very well on image, audio, and textual data, Easily updated with new data	Not suitable for classical machine learning problems.
Algorithms are easier to interpret, have more theories to back them up	Labor intensive model maintenance	Versatile architecture and low overhead maintenance	Computationally intensive to train, and they require much more expertise to tune

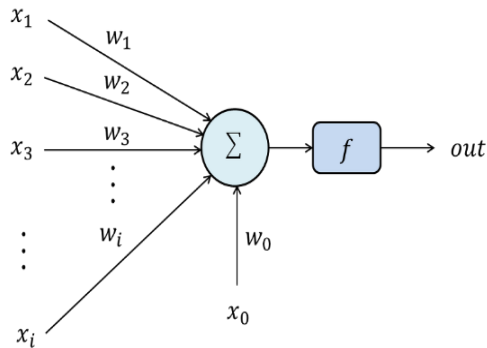


NEURAL NETWORKS MODEL

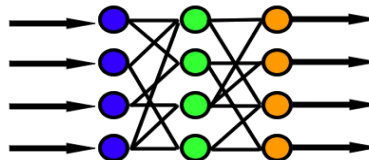
Feed forward neural network (FNN)

the information moves in only forward direction from the input nodes to the output nodes. There are no cycles or loops in the network.;

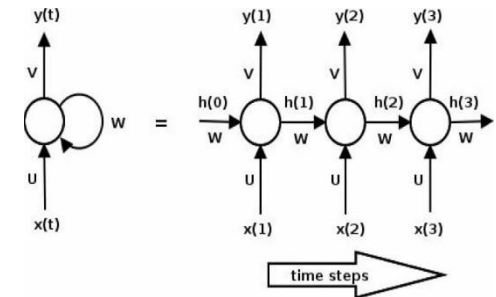
Deep FNN consists of tens of layers and thousands of nodes; the simplest kind of FNN is logistic model



Logistic Model



Feedforward Neural Network



Recurrent Neural Network

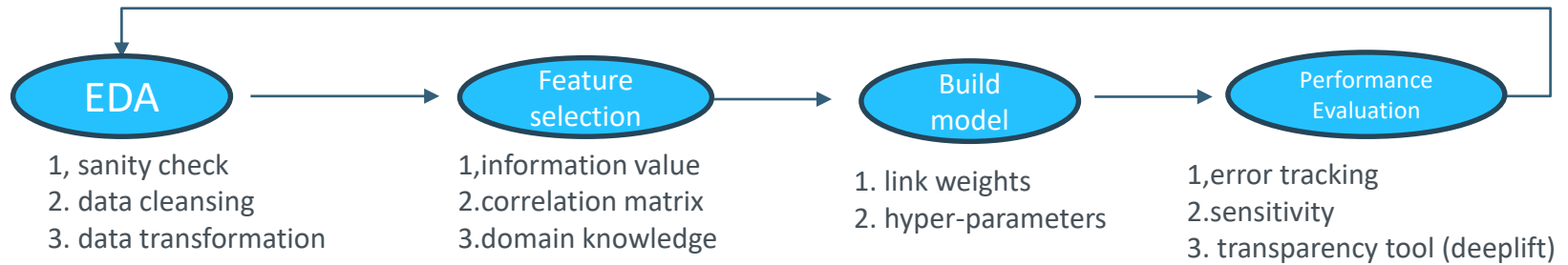
Recurrent Neural Network (RNN)

A class of neural networks exploit the historical input sequences. Such inputs could be text, speech, time series, and anything else where the occurrence of an input in the sequence y is dependent on the inputs that appeared before it

Motivation: Not all problems can be converted into one with fixed length inputs and outputs, such as text translation, speech recognition or time-series; predictions require a system to store and use context information

The input at time t include both the attributes at t and the intermediate values containing history at $t-1$.

BUILDING NEURAL NETWORK MODEL



Deep neural network fitting

2003-2018 30yr agency MBS data (~25G data)

30+ input variables: pool attributes, macro-economic variables

To reduce complexity, we added incentive, 1 regime indicators, and 1 policy indicator (HARP)

Cost function of RMS error of pool level prepayment

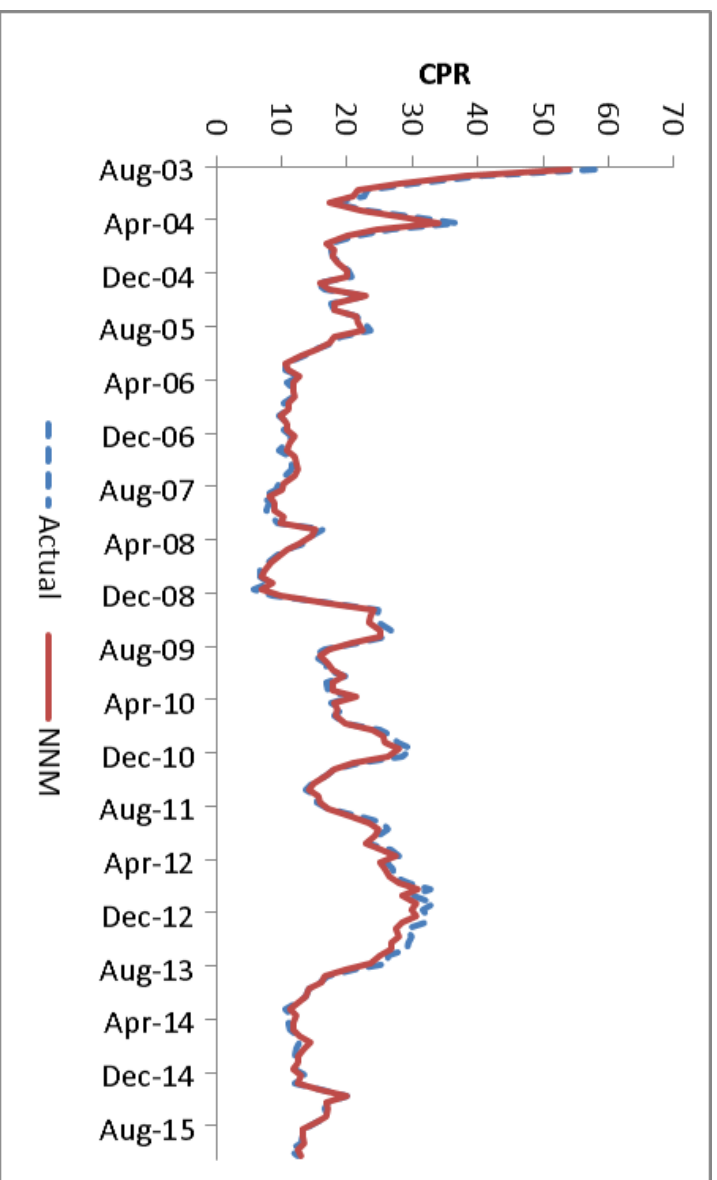
1 round of fitting can be completed in ~ 3 hours on a GPU machine

MODEL DRIVERS

Independent variables	
WALA	Weighted Average Loan Age
WAC	Weighted Average Coupon
CLNSZ	Current Average Loan Size
OLTV	Original Loan to Value
Refi%	Percentage of Refinanced Loans by UPB
SecHome%	Percentage of Second Home Loans by UPB
MultiFamily%	Percentage of Muti Family Loans by UPB
Investor%	Percentage of Investor Loans by UPB
TPO%	Percentage of Third party origination by UPB
AOL	Original Average Loan Size
LNSZ_Q4	Max original loan size
LNSZ_Q3	Max original Loan Size - 3rd Quartile
LNSZ_Q1	Max original Loan Size - 1st Quartile
Geo_CA%	Percentage of California Loans by UPB
Geo_FL%	Percentage of Florida Loans by UPB
Geo_TX%	Percentage of Texas Loans by UPB
Geo_NY%	Percentage of New York Loans by UPB
Geo_NE%	Percentage of New England Region Loans by UPB
Geo_NO%	Percentage of North Region Loans by UPB
Geo_SO%	Percentage of South region Loans by UPB
Geo_PC%	Percentage of Pacific region Loans by UPB
Geo_AT%	Percentage of Atlantic region Loans by UPB
Geo_NONUS%	Percentage of non-US region Loans by UPB
Seasonality	Calendar month

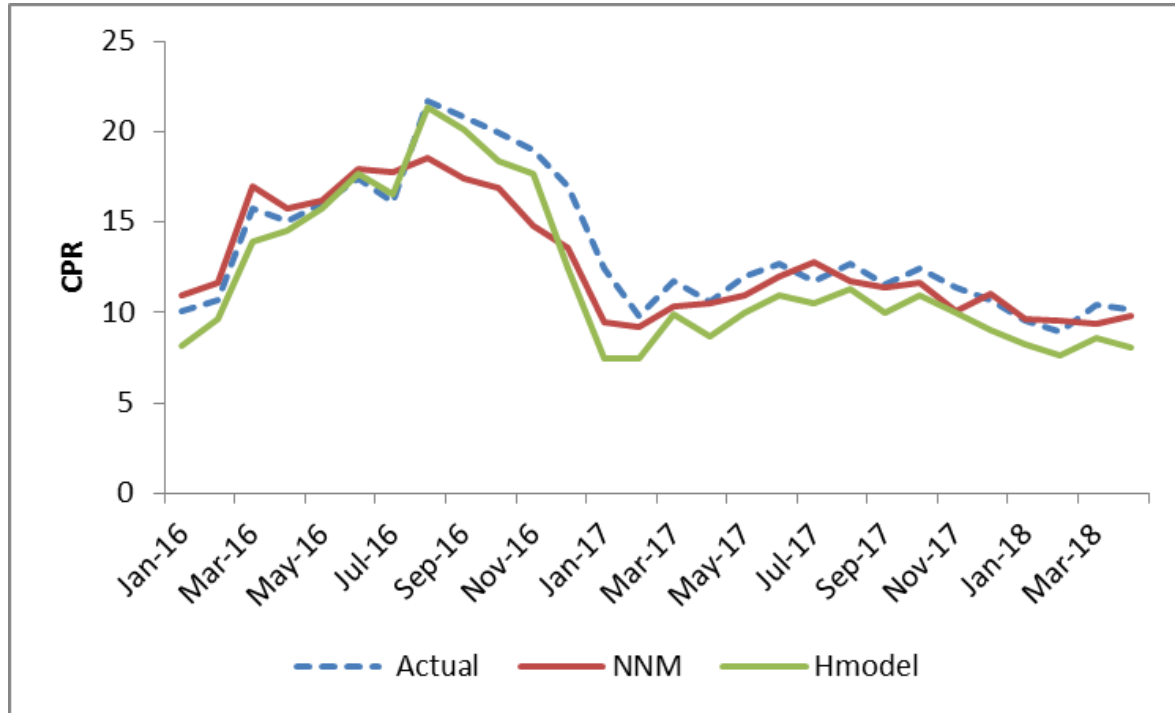
Derived Variables	
Incentive	WAC - Mortgage Rate(t)
Rolling Incentive	Average Incentive (20month) $\sum_{t=1}^{t=\min(20,wala)} Incentive / \min(20,w$
Loan size dispersion	(LNSZ_Q3-LNSZ_Q1)/AOL
SATO	Spread-at_ origination = WAC - Mortgage Rate(0)
HPA	House Price Appreciation (HPI(t)/HPI(0)-1) and Dec. 2011
HARP-able	2: IssueMonth <= Jun. 2009 and factor date > Dec. 2011
HARP-ed	Refi% = 100 and OLTV > 80 and issueMonth > Jun. 2009
Underwriting standard	0: before 2008, 1: after 2008
Weight	
cBal	Current Balance
Dependent Variable	
Prepayment speed	Prepayment speed in SMM

AGENCY 30YR UNIVERSE SPEEDS ERROR TRACKING



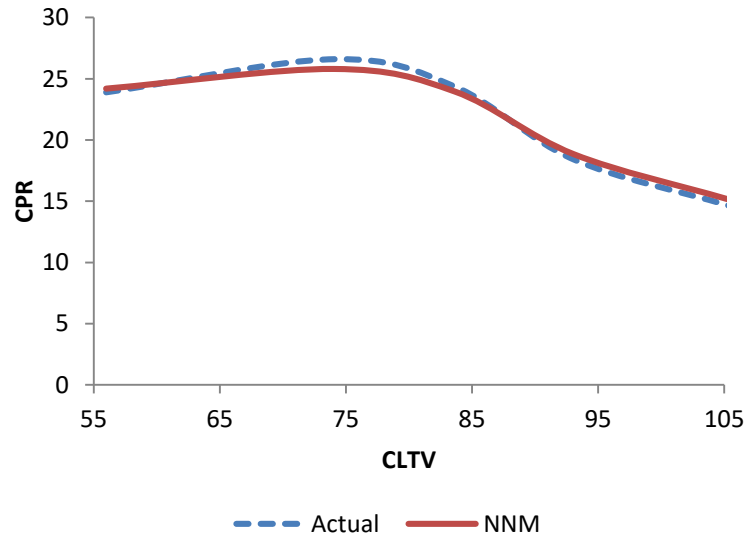
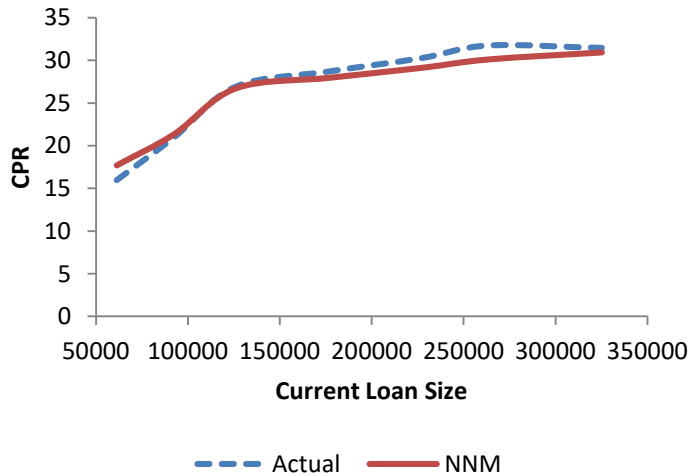
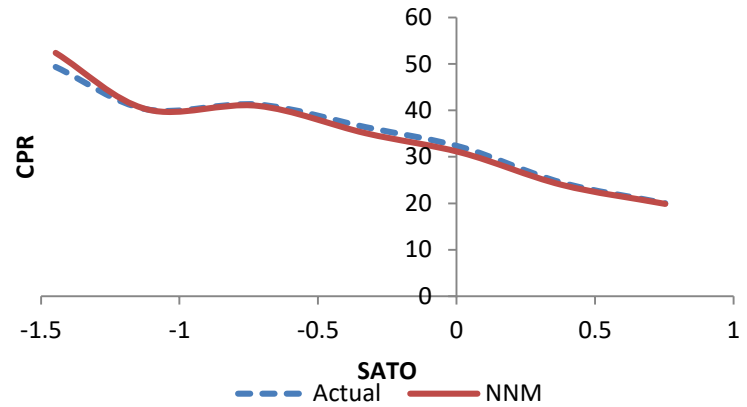
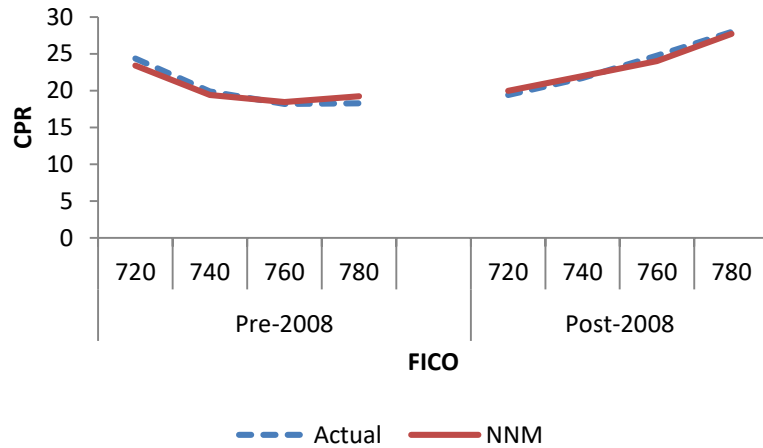
- Training Data: 2003 – 2015 Dec. Random sample 10% pools.
- Error tracking is generated using out-of-the-sample pools.

OUT-OF-SAMPLE FORECASTS

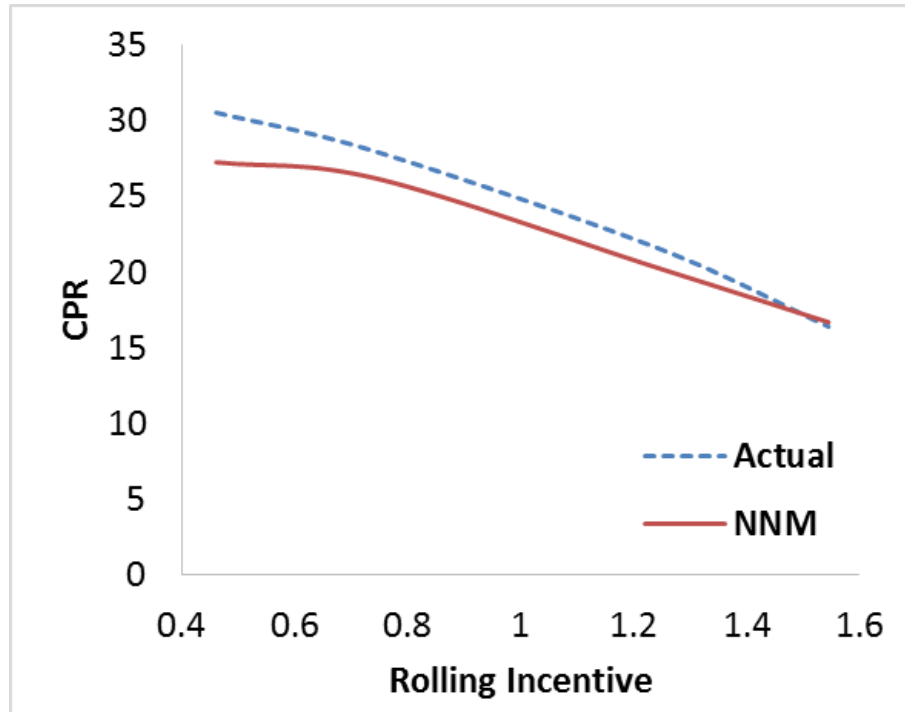


- True out-of-time and out-of-sample test.
- Overall fitting is good in out-of-sample test
- Missed the refi wave in second half of 2016

MODEL RISK FACTORS



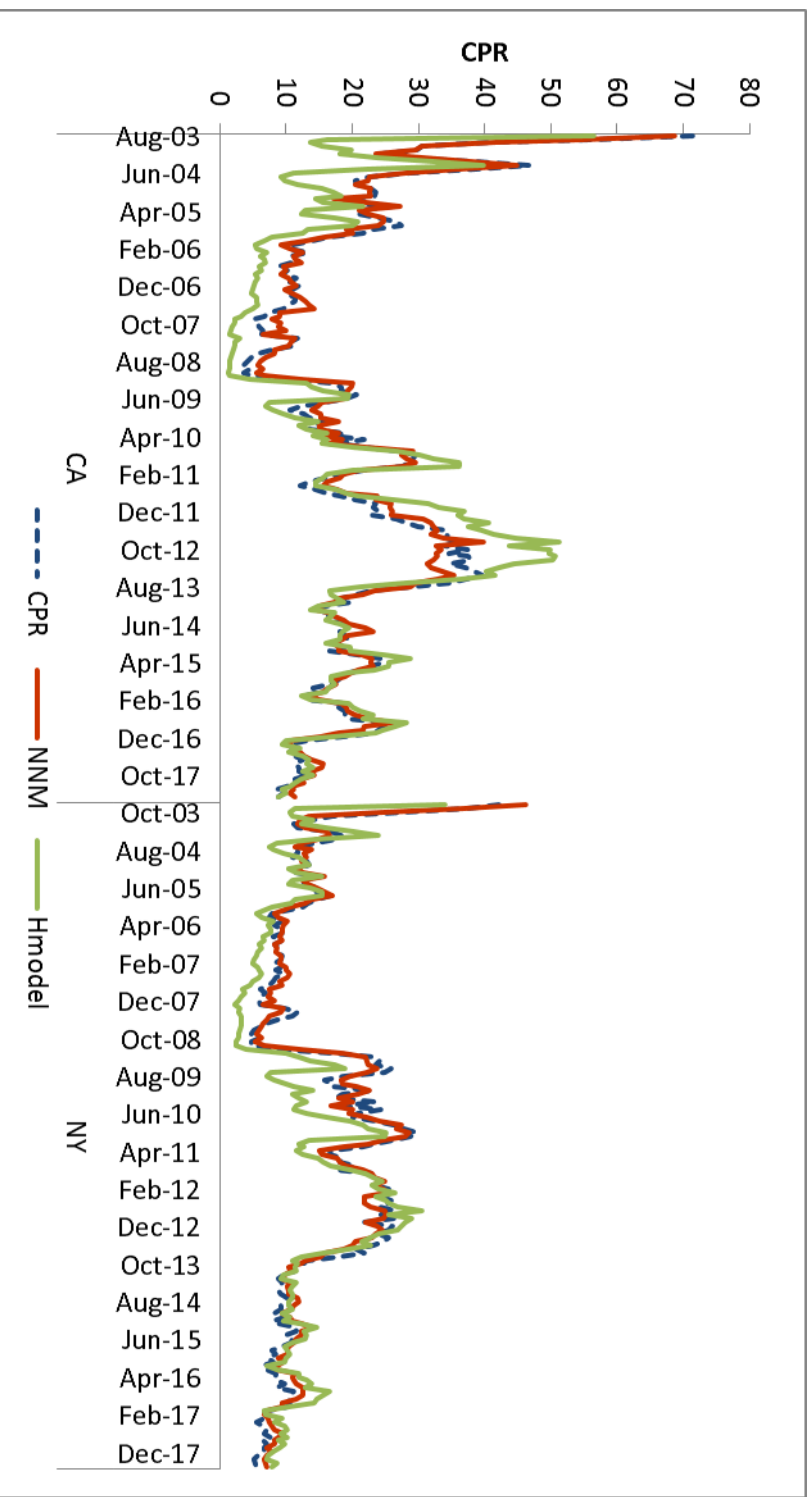
MODEL BURNOUT



NNM and actual prepayment speeds against average incentive in prior 20 months

MODEL POOL VARIABLES VS “HUMAN” MODEL

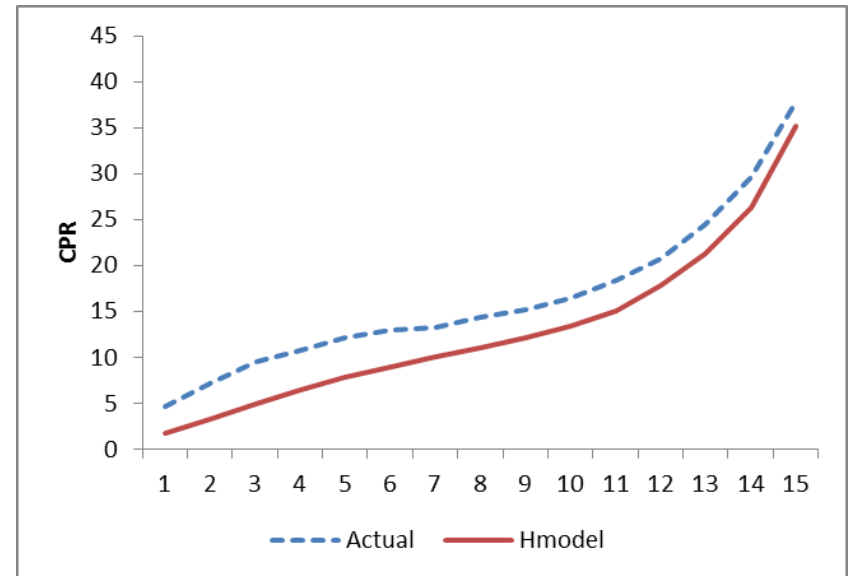
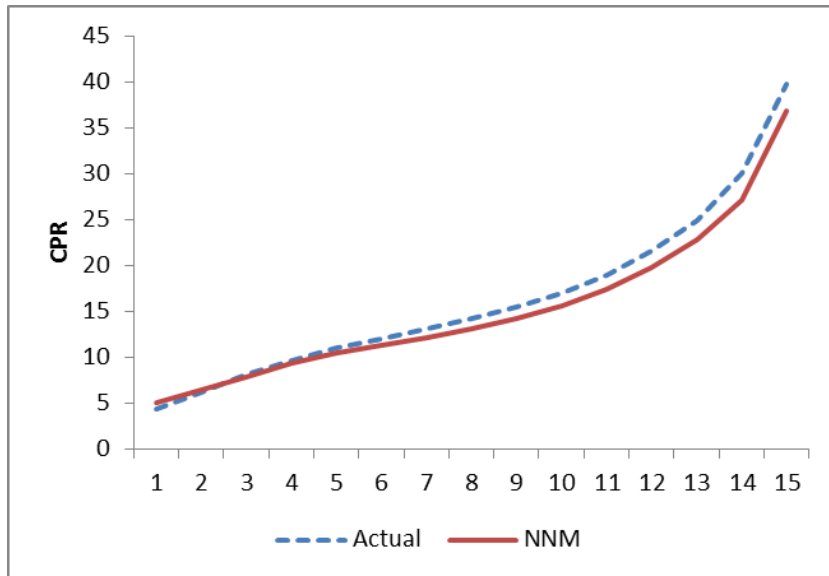
NNM and Hmodel Error Tracking against State Variables



NNM accurately captured state-level prepayment behaviors

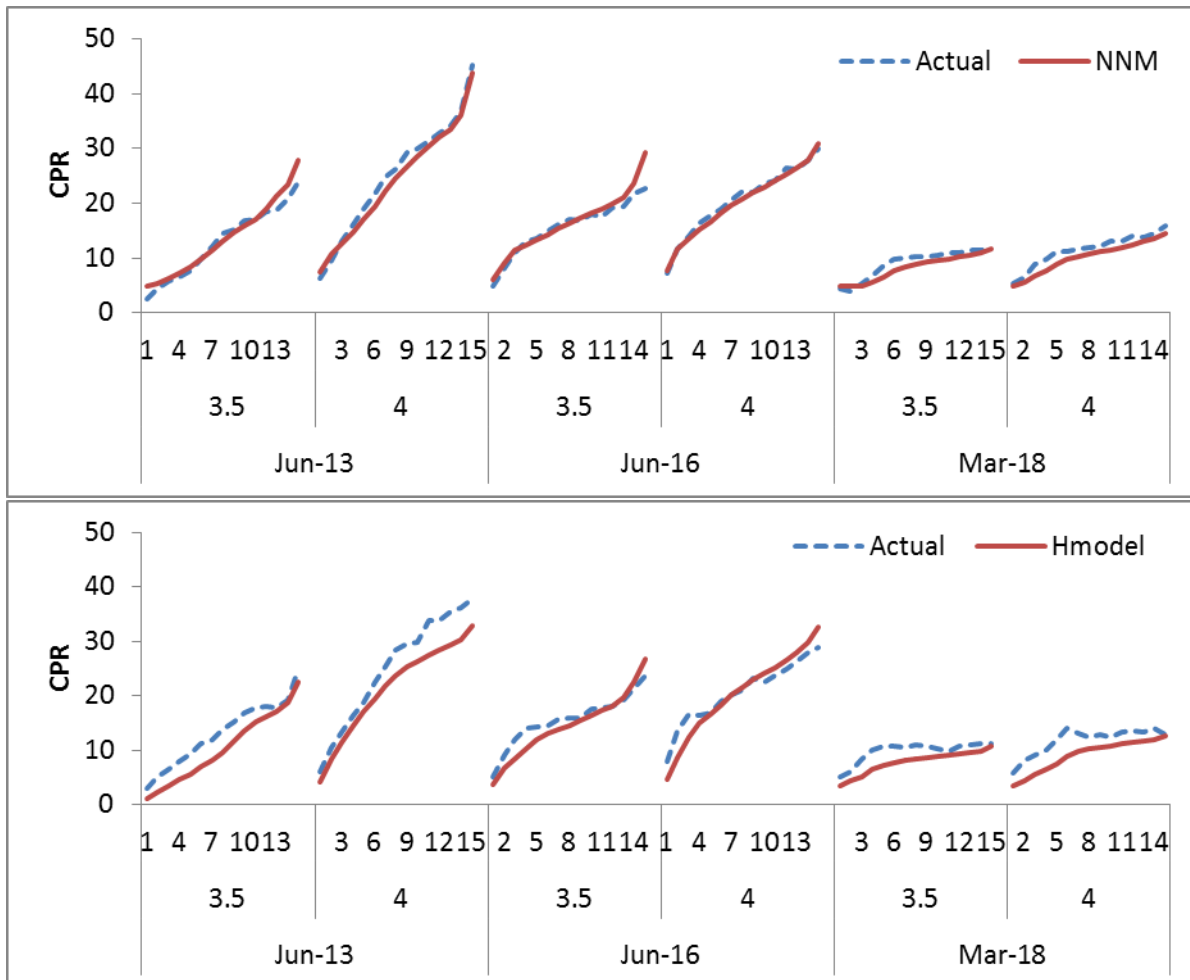
MODEL POOL VARIABLES VS HUMAN MODEL

Ranking-Based Sample Error Tracking for Coupon 4s



- Ranking based error tracking methodology provides a comprehensive measure of model accuracy across all pool variables
- NNM performed better than Hmodel

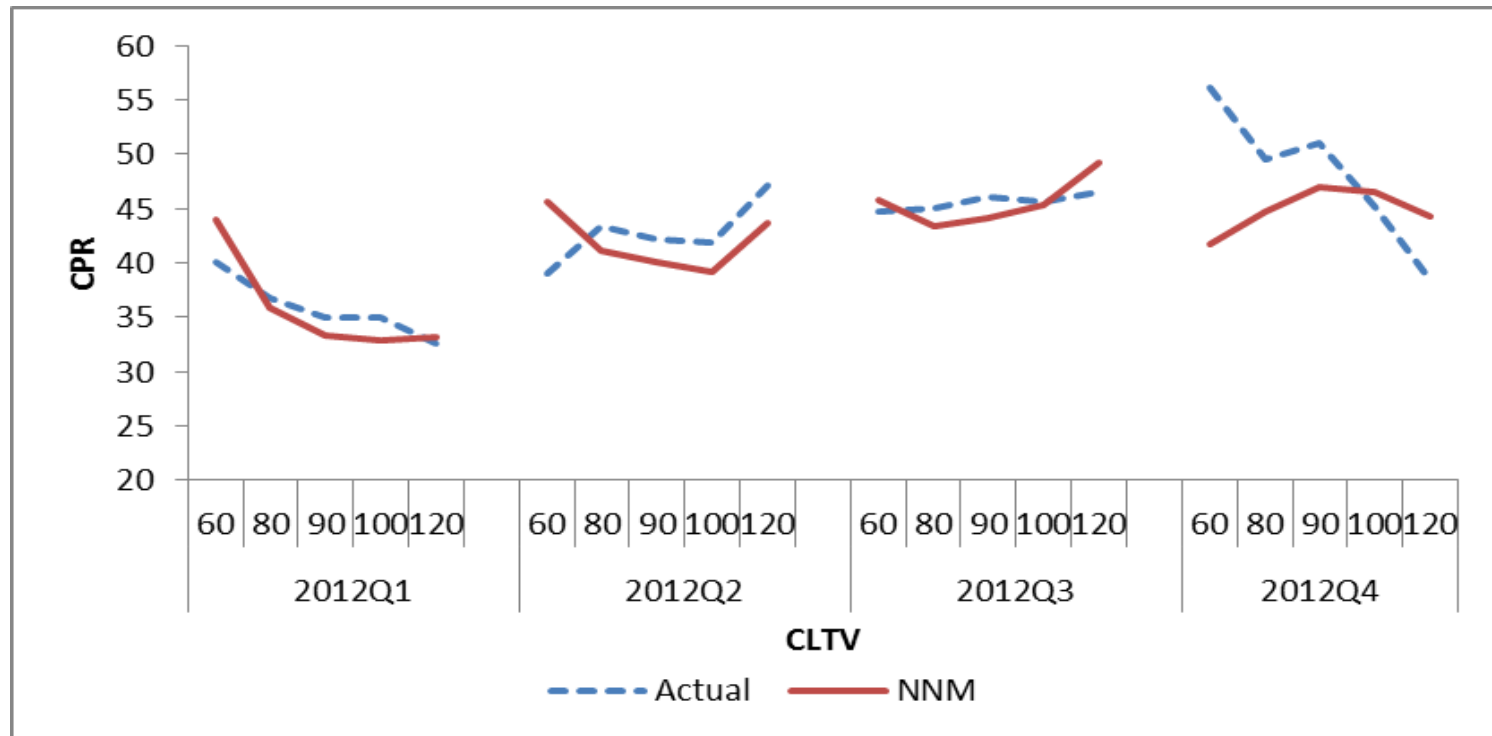
MODEL POOL VARIABLES VS HUMAN MODEL



Sample ranking-based error tracking at different time point

MODEL HARP EFFECTIVENESS

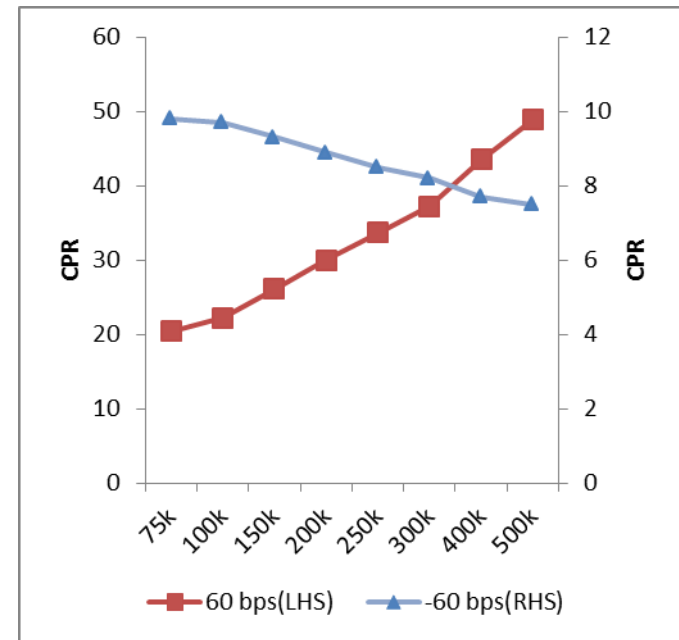
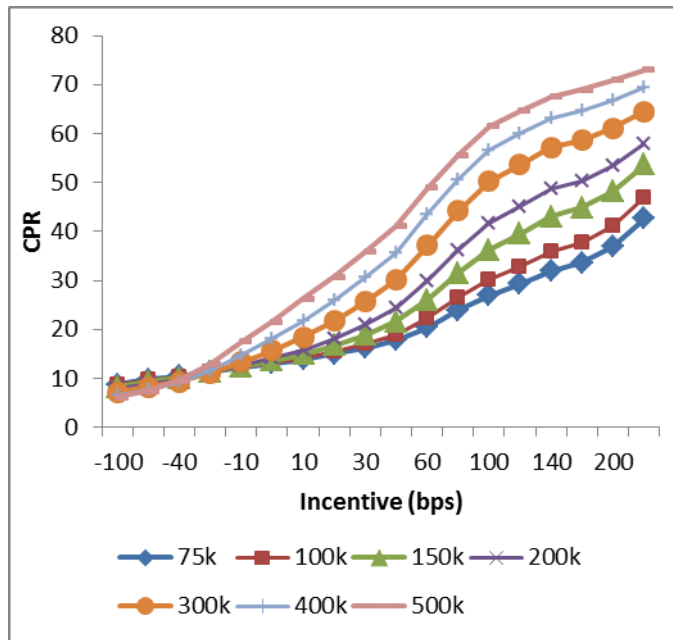
Error Tracking against HARP effectiveness across CLTV Cohorts



NNM is able to pick up the general trend of HARP effectiveness but missed the complexity of its revolution

MODEL SENSITIVITY

Model prepayment sensitivity to loan sizes and refinance Incentives



NNM captured the prepayment behavior for loan size

“MEDIA EFFECT”

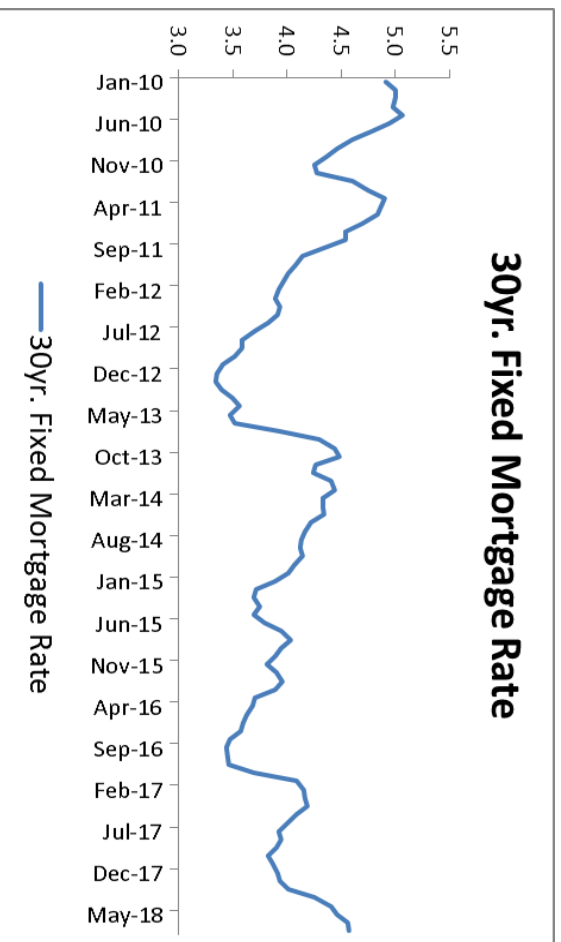
FH 2011 3.5 vs 2010 4 comparisons, across TPO/Retail and Refi/Purchase combinations

Cohort	Observation Range	CPR	WALA	SATO	CLTV	CLNSZ	Incentive	FICO	Avg. UPB(bn)
Purchase/Retail									
FH 3.5 2011	Jul.12 - Dec. 12	16.1	13	-5	77	212258		52	770
FH 4 2010	Nov. 11 - Feb. 12	13.9	15	3	78	201901		45	767
Purchase/TPO									
FH 3.5 2011	Jul.2012 - Dec. 12	21.9	12	-3	76	235847		50	770
FH 4 2010	Nov. 11 - Feb. 12	16.4	16	3	78	224734		45	765
Refi/Retail									
FH 3.5 2011	Jul.12 - Dec. 12	29.2	12	-2	66	216270		54	771
FH 4 2010	Nov. 11 - Feb. 12	15.3	15	11	70	208962		52	766
Refi/TPO									
FH 3.5 2011	Jul.12 - Dec. 12	46.1	12	-8	64	269298		46	773
FH 4 2010	Nov. 11 - Feb. 12	26.2	15	2	69	245496		44	767
									23.02

2011 3.5s and 2010 4s prepayment speeds are compared across loan attributes, loan purpose and origination channel

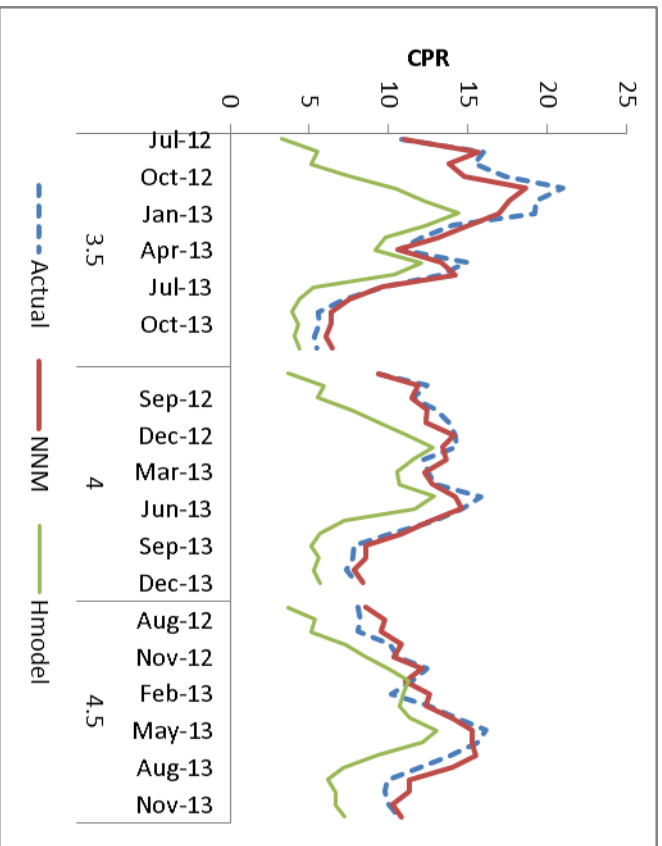
3.5s is much faster than 4s given similar loan attributes and incentive

30yr. Fixed Mortgage Rate

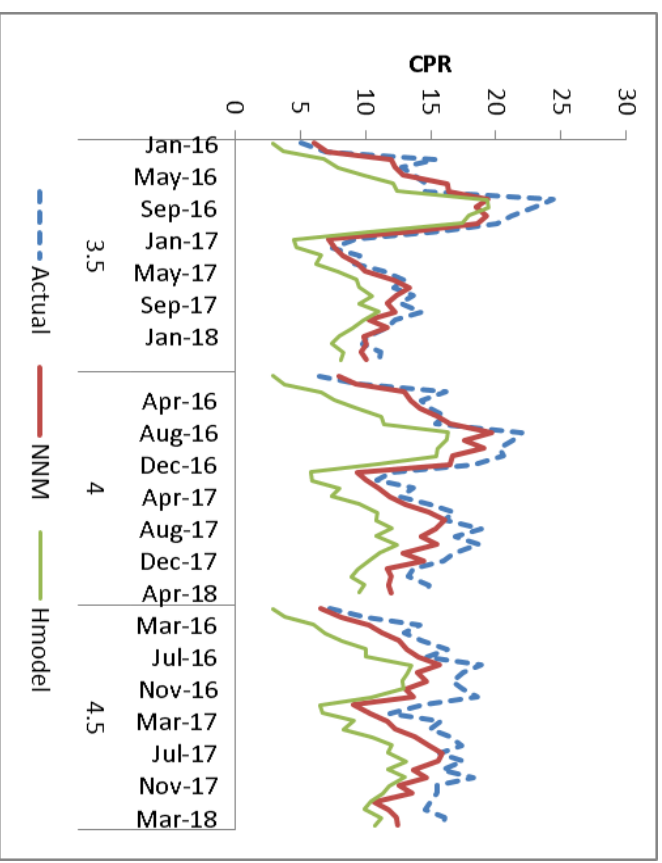


MODEL “MEDIA EFFECT”

2012 Vintage in 2012 refinance wave

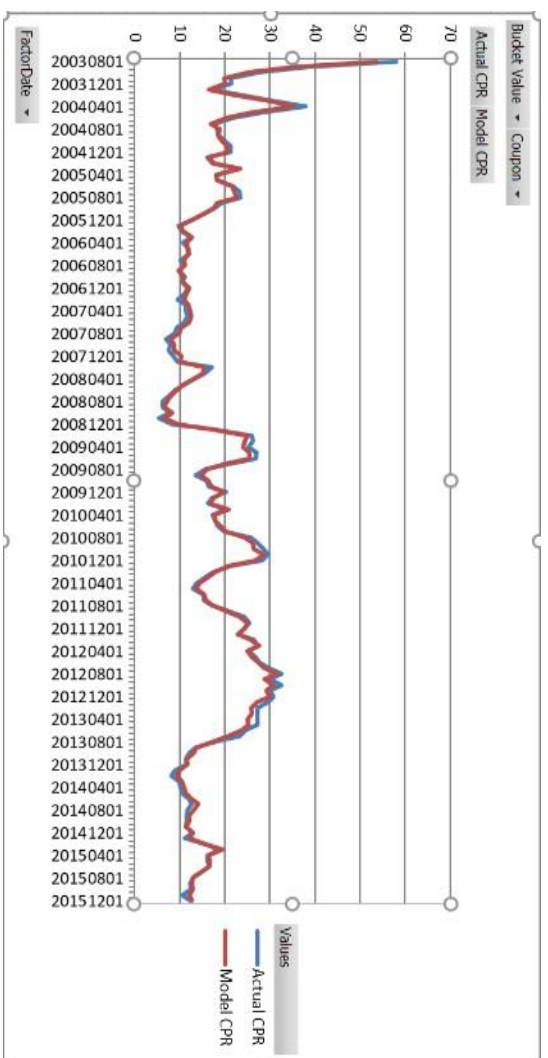


2015 Vintage in 2016 refinance wave



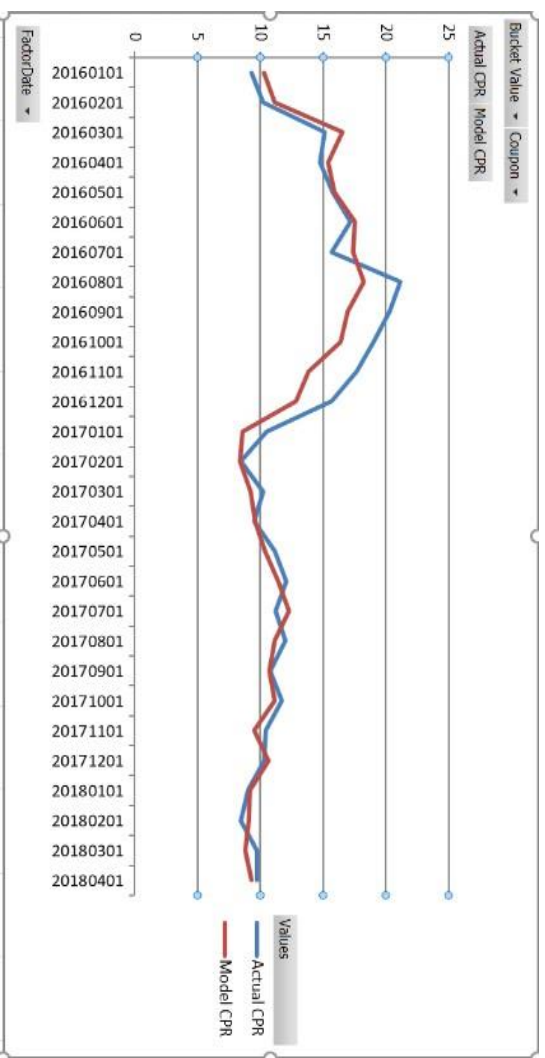
MODEL ERROR TRACKING

In-time
Out-of-sample
(1/2003-12/2015)



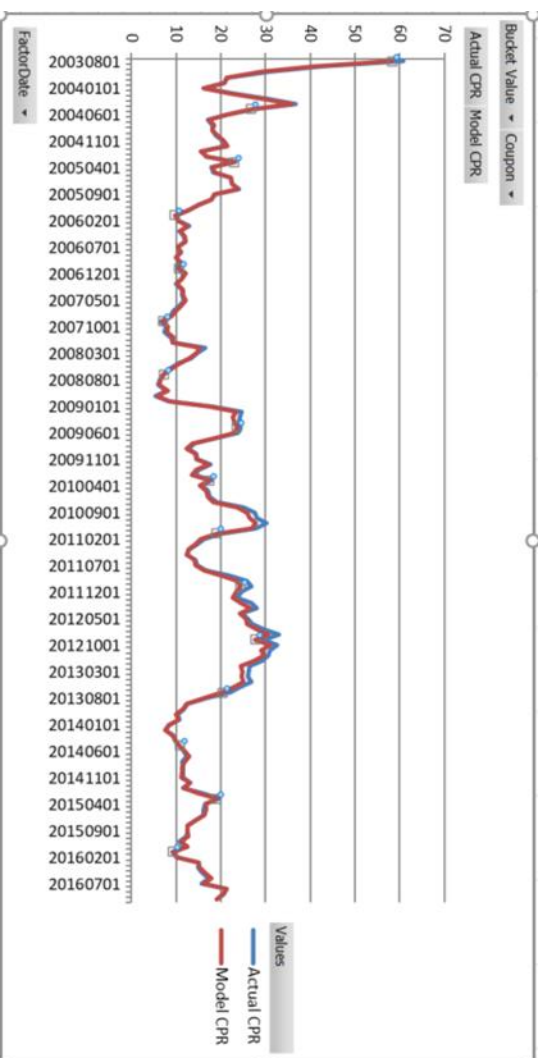
1. All attributes statistics are very close on July and August 2016 except CPR.
2. Risk driver is missing, i.e., media effect or regime change

Out-of-time
Out-of-sample
(1/2016-4/2018)

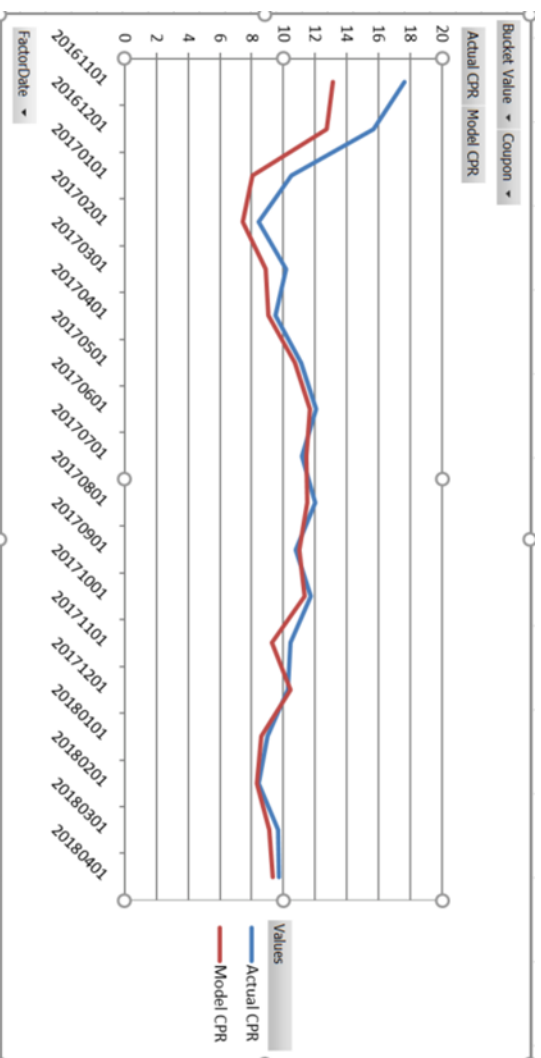


MODEL ERROR TRACKING

In-time
Out-of-sample
(1/2003-10/2016)



Out-of-time
Out-of-sample
(11/2016-4/2018)

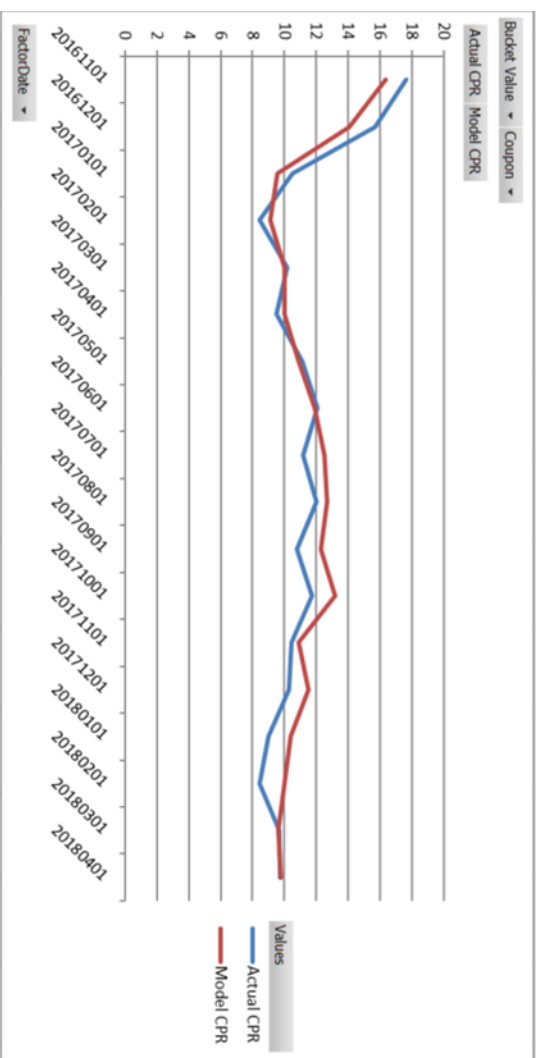
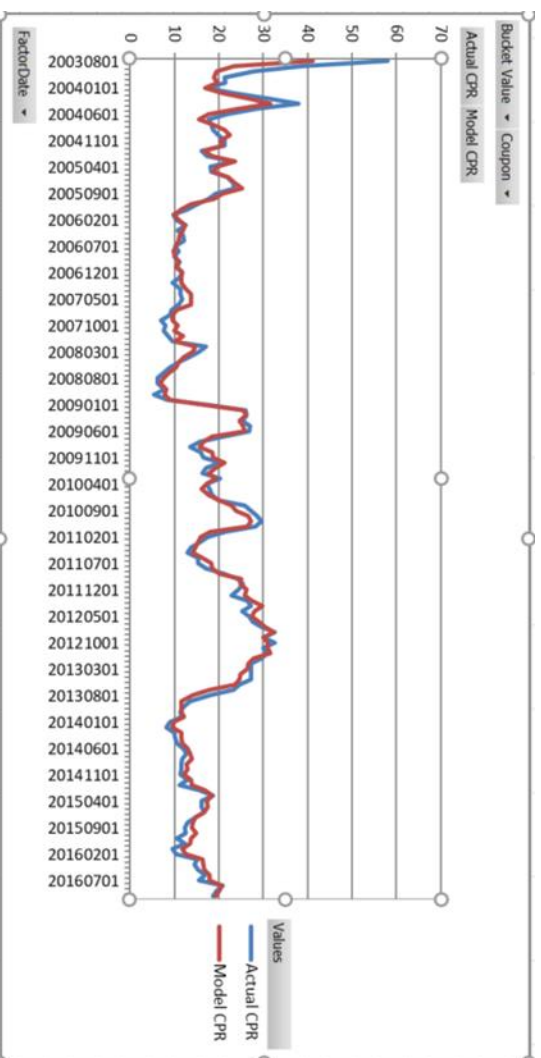


MODEL ERROR TRACKING

In-time
Out-of-sample
(1/2003-10/2016)

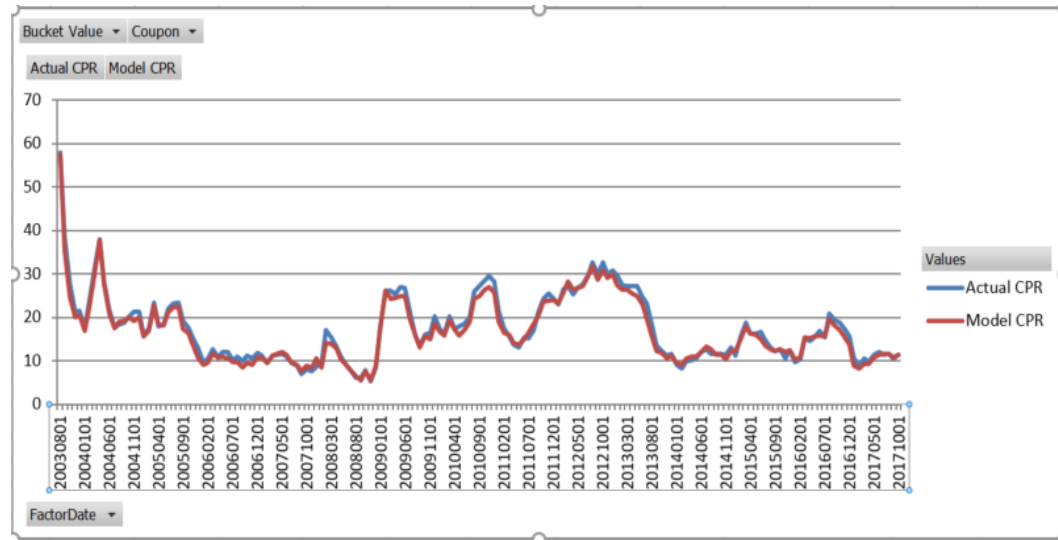
- When Increase weights on 8/2016 – 10/2016 by 40 times in training:
1. Better in the early stage of out-of-time test
 2. Sacrifice other period.

Out-of-time
Out-of-sample
(11/2016-4/2018)

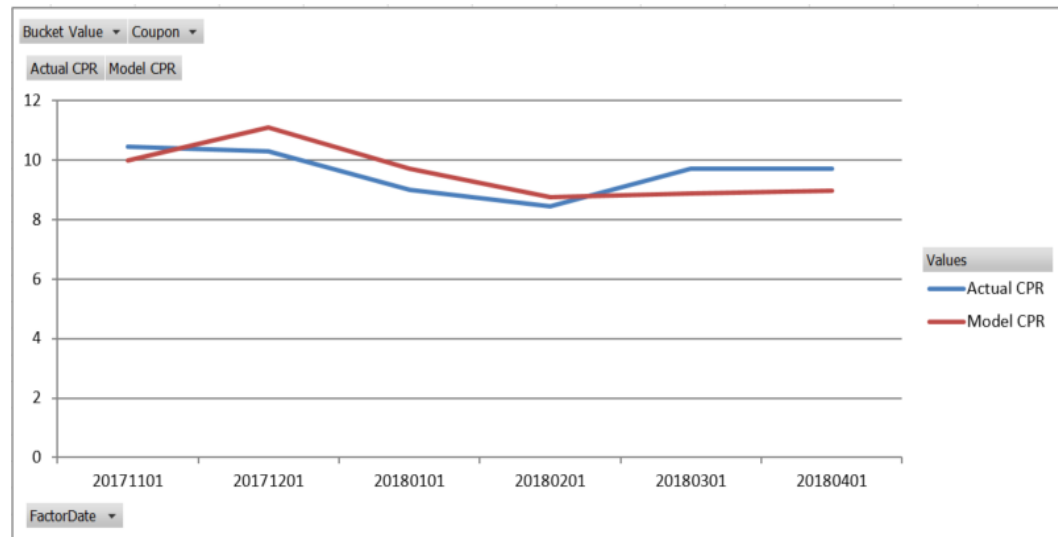


MODEL ERROR TRACKING

In-time
Out-of-sample
(1/2003-10/2017)



Out-of-time
Out-of-sample
(10/2017-4/2018)



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AMERICAS		EUROPE, MIDDLE EAST & AFRICA		ASIA PACIFIC	
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				Tokyo	+81 3 5290 1555

• = toll free

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